Summary of Gas Laws

$PV = nRT$

Boyle's Law

$$\frac{P_1V_1}{P_2} = \frac{P_2V_2}{P_2}$$

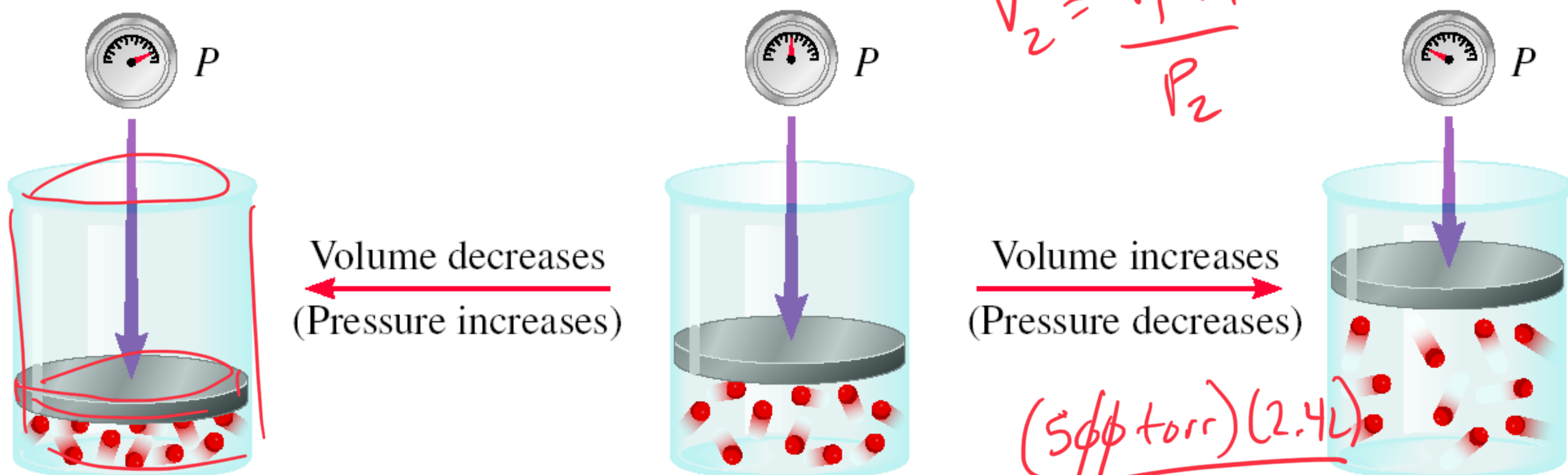
$P_1 = 500$ torr

$V_1 = 2.4$ L

$P_2 = 800$ torr

$$V_2 = \frac{P_1V_1}{P_2}$$

Increasing or decreasing the volume of a gas at a constant temperature



Boyle's Law

$P = (nRT)\frac{1}{V}$ nRT is constant

$$\frac{(5\cancel{0}\cancel{0}\text{ torr})(2.4\text{L})}{8\cancel{0}\cancel{0}\text{ torr}}$$

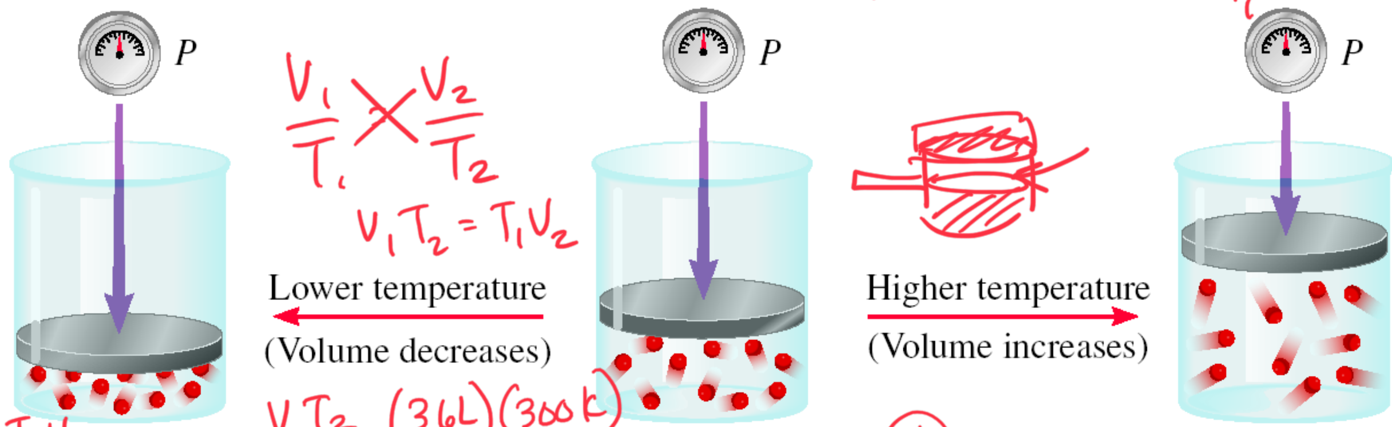
$$\frac{12}{8} = \boxed{1.5\text{L}}$$

Charles Law

Heating or cooling a gas at constant pressure

$\frac{PV}{T} = nR$

$\frac{P_1V_1}{T_1} = \frac{P_2V_2}{T_2}$



$\frac{V_1}{T_1} = \frac{V_2}{T_2}$

$V_1T_2 = T_1V_2$

$\frac{V_1T_2}{T_1} = \frac{T_1V_2}{T_1}$

$V_2 = \frac{V_1T_2}{T_1} = \frac{(3.6L)(300K)}{250K} = \boxed{4.32L}$

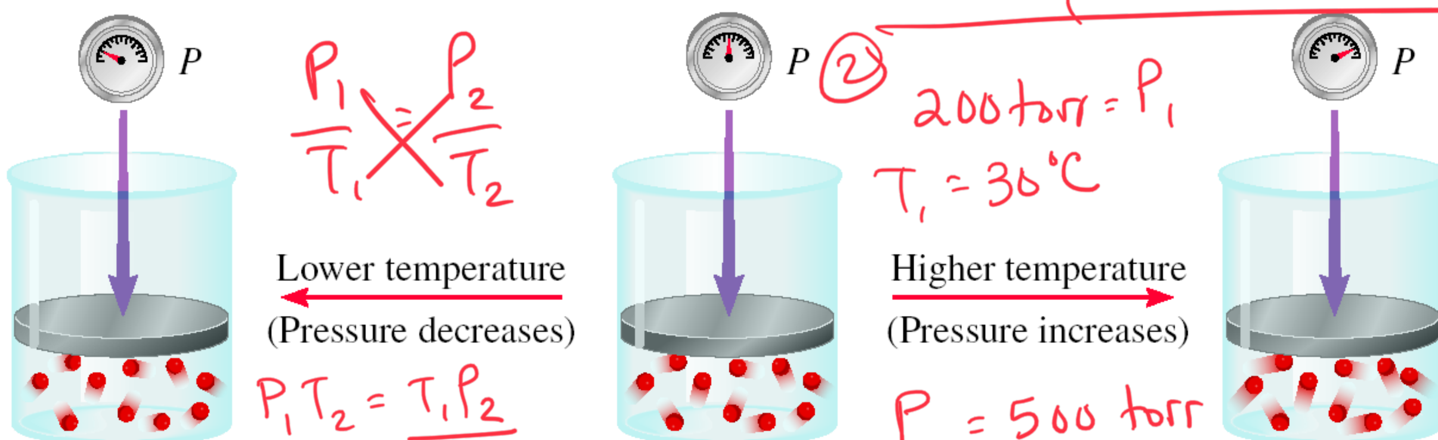
Charles's Law

$V = \left(\frac{nR}{P}\right) T \quad \frac{nR}{P}$ is constant

① $V_1 = 3.6L$ $T_2 = 300K$

$T_1 = 250K$

Heating or cooling a gas at constant volume



$\frac{P_1}{T_1} = \frac{P_2}{T_2}$

② 200 torr $= P_1$

$T_1 = 30°C$

$\frac{P_1T_2}{P_1} = \frac{T_1P_2}{P_1}$

$P_2 = 500$ torr

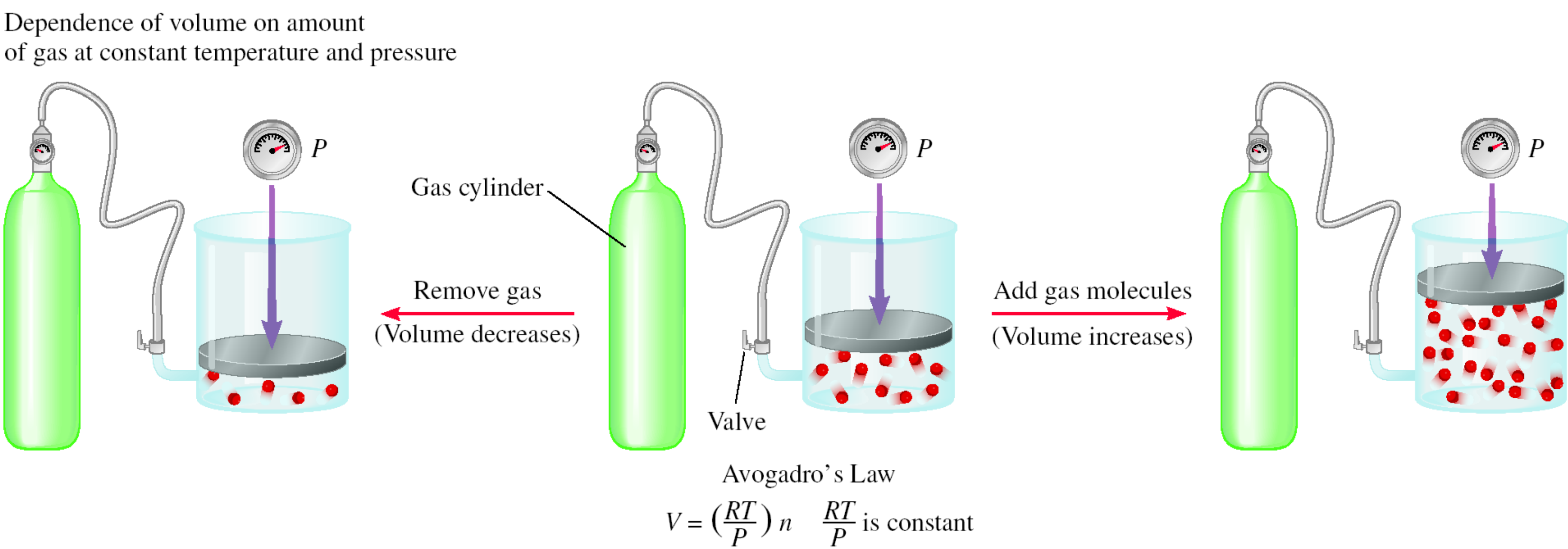
Charles's Law

$P = \left(\frac{nR}{V}\right) T \quad \frac{nR}{V}$ is constant

$T_1 = 30 + 273 = 303$

$T_2 = \frac{T_1P_2}{P_1} = \frac{(303K)(500 \text{ torr})}{200 \text{ torr}} = \boxed{757K}$

Avogadro's Law



Ideal Gas Equation

Boyle's law: $P \propto \frac{1}{V}$ (at constant *n* and *T*)

Charles' law: $V \propto T$ (at constant *n* and *P*)

Avogadro's law: $V \propto n$ (at constant *P* and *T*)

$$V \propto \frac{nT}{P}$$

$$V = \text{constant x } \frac{nT}{P} = R \frac{nT}{P}$$

R is the **gas constant**

$$\boxed{PV = nRT}$$

The conditions 0 ^{0}C and 1 atm are called **standard temperature and pressure (STP).**

Experiments show that at STP, 1 mole of an ideal gas occupies 22.414 L.

$$PV = nRT$$

$$R = \frac{PV}{nT} = \frac{(1\text{ atm})(22.414\text{L})}{(1\text{ mol})\boxed{(273.15\text{ K})}}$$

$$R = 0.082057\text{ L} \bullet \text{atm} / (\text{mol} \bullet \text{K})$$

What is the volume (in liters) occupied by 49.8 g of HCl at STP?

$T = 0\ ^0\mathrm{C} = 273.15\ \mathrm{K}$

$P = 1\ atm$

$$PV = nRT$$

$$V = \frac{nRT}{P}$$

$$n = 49.8\ \mathrm{g} \times \frac{1\ \mathrm{mol\ HCl}}{36.45\ \mathrm{g\ HCl}} = 1.37\ \mathrm{mol}$$

$$V = \frac{1.37\ \cancel{\mathrm{mol}} \times 0.0821\ \frac{\mathrm{L}\bullet\cancel{\mathrm{atm}}}{\cancel{\mathrm{mol}}\bullet\cancel{\mathrm{K}}} \times 273.15\ \cancel{\mathrm{K}}}{1\ \cancel{\mathrm{atm}}}$$

$$V = 30.7\ \mathrm{L}$$

Argon is an inert gas used in lightbulbs to retard the vaporization of the filament. A certain lightbulb containing argon at 1.20 atm and 18 ^{0}C is heated to 85 ^{0}C at constant volume. What is the final pressure of argon in the lightbulb (in atm)?

$$PV = nRT \qquad n,\ V \text{ and } R \textbf{ are constant}$$

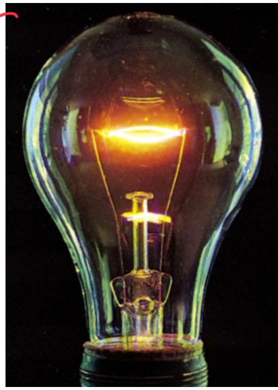
$$\frac{nR}{V} = \frac{P}{T} = \text{constant}$$

$P_1 = 1.20$ atm $\qquad P_2 = ?$

$T_1 = 291$ K $\qquad T_2 = 358$ K

$$\frac{P_1}{T_1} = \frac{P_2}{T_2}$$

$$P_2 = P_1\, x\ \frac{T_2}{T_1} = 1.20 \text{ atm x } \frac{358\ \cancel{\text{K}}}{291\ \cancel{\text{K}}} = 1.48 \text{ atm}$$



Density (d) Calculations

$n = mol$

$$\boxed{d} = \boxed{\frac{m}{V}} = \frac{P\mathcal{M}}{RT}$$

m is the mass of the gas in g

$\mathcal{M}$ is the molar mass of the gas

$d = \frac{m}{V}$

$\frac{PV}{V} = \frac{nRT}{V}$

$\mathcal{M} = \frac{mass}{mol}$

Molar Mass ($\mathcal{M}$) of a Gaseous Substance

$\mathcal{M} = \frac{m}{n}$ $n = \frac{m}{\mathcal{M}}$

$$\mathcal{M} = \frac{dRT}{P}$$

d is the density of the gas in g/L

$P = \frac{nRT}{V}$ $P = \frac{mRT}{V\mathcal{M}} = P = \frac{dRT}{\mathcal{M}}$

$\frac{P\mathcal{M}}{RT} = d$

(10) A 2.10-L vessel contains 4.65 g of a gas at 1.00 atm and 27.0 ºC. What is the molar mass of the gas?

$$M = \frac{\text{molar}}{\text{mass}} = \frac{dRT}{P} = \frac{mRT}{PV}$$

$$M = \frac{dRT}{P} \qquad d = \frac{m}{V} = \frac{4.65\text{ g}}{2.10\text{ L}} = 2.21\ \frac{\text{g}}{\text{L}}$$

R

$$M = \frac{2.21\frac{\text{g}}{\cancel{\text{L}}} \times \boxed{0.0821\frac{\cancel{\text{L}}\bullet\cancel{\text{atm}}}{\text{mol}\bullet\cancel{\text{K}}}} \times 300.15\ \cancel{\text{K}}}{1\ \cancel{\text{atm}}}$$

27+273

300 K

$$M = \frac{mRT}{PV} = \frac{(4.65g)(300K)(0.082)}{(1\,atm)(2.10L)} = \boxed{54.5\ g/mol}$$

molar mass

M = 54.5 g/mol

Gas Stoichiometry

Amount of reactant (grams or volume) → Moles of reactant → Moles of product → Amount of product (grams or volume)

What is the volume of CO_2 produced at 37 ^{0}C and 1.00 atm when 5.60 g of glucose are used up in the reaction:

$$C_6H_{12}O_6\ (s) + 6O_2\ (g) \longrightarrow 6CO_2\ (g) + 6H_2O\ (l)$$

2

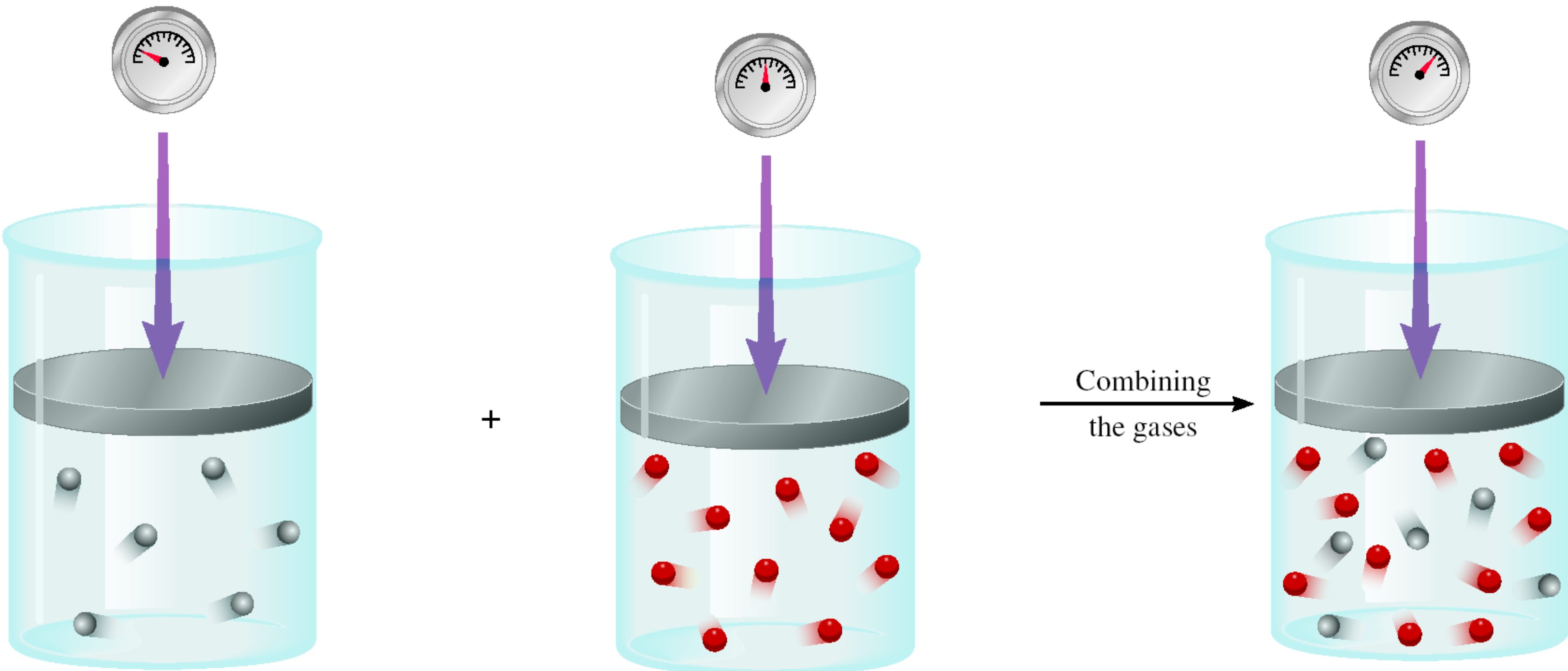
$$\text{g } C_6H_{12}O_6 \longrightarrow \text{mol } C_6H_{12}O_6 \longrightarrow \text{mol } CO_2 \longrightarrow V\ CO_2$$

$$5.60\ \cancel{\text{g } C_6H_{12}O_6} \times \frac{1\ \cancel{\text{mol } C_6H_{12}O_6}}{180\ \cancel{\text{g } C_6H_{12}O_6}} \times \frac{6\ \text{mol } CO_2}{1\ \cancel{\text{mol } C_6H_{12}O_6}} = 0.187\ \text{mol } CO_2$$

$$\boxed{V} = \frac{nRT}{P} = \frac{0.187\ \cancel{\text{mol}} \times 0.0821\ \dfrac{\text{L}\bullet\cancel{\text{atm}}}{\cancel{\text{mol}}\bullet\cancel{\text{K}}} \times 310.15\ \cancel{\text{K}}}{1.00\ \cancel{\text{atm}}} = 4.76\ \text{L}$$

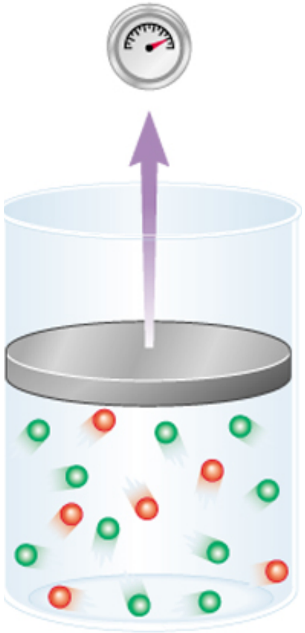
Dalton's Law of Partial Pressures

V and T are **constant**



P_1 $\qquad$ P_2 $\qquad$ $P_{\text{total}} = P_1 + P_2$

Consider a case in which two gases, A and B, are in a container of volume V.



$$P_A = \frac{n_A RT}{V}$$

n_A is the number of moles of A

$$P_B = \frac{n_B RT}{V}$$

n_B is the number of moles of B

$$P_T = P_A + P_B \qquad X_A = \frac{n_A}{n_A + n_B} \qquad X_B = \frac{n_B}{n_A + n_B}$$

$$P_A = X_A P_T \qquad P_B = X_B P_T$$

$$\boxed{P_i = X_i P_T}$$

mole fraction (X_i) = $\dfrac{n_i}{n_T}$

A sample of natural gas contains 8.24 moles of CH_4, 0.421 moles of C_2H_6, and 0.116 moles of C_3H_8. If the total pressure of the gases is 1.37 atm, what is the partial pressure of propane (C_3H_8)?

$$P_{C_2H_6} \quad \frac{0.421}{8.24 + 0.421 + 0.116} = 0.04797$$

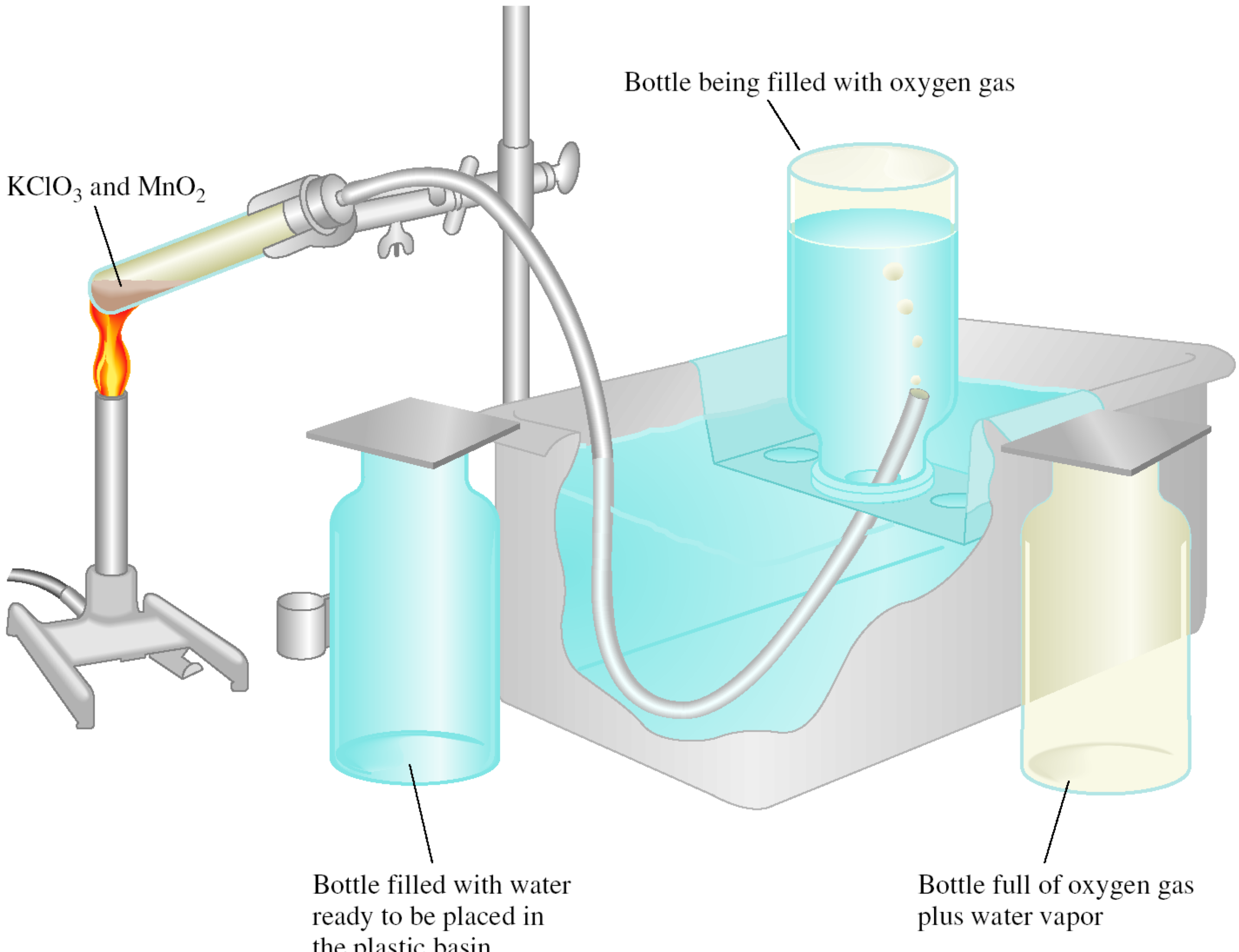
$$0.04797(1.37)$$

$$P_i = X_i P_T \qquad P_T = 1.37 \text{ atm} \qquad = \boxed{0.0657 \text{ atm}}$$

$$X_{\text{propane}} = \frac{0.116}{8.24 + 0.421 + 0.116} = 0.0132$$

$$P_{\text{propane}} = 0.0132 \text{ x } \boxed{1.37 \text{ atm}} \qquad = 0.0181 \text{ atm}$$

Collecting a Gas over Water



$$2KClO_3\ (s) \longrightarrow 2KCl\ (s) + 3O_2\ (g)$$

$$P_T = P_{O_2} + P_{H_2O}$$

Vapor of Water and Temperature

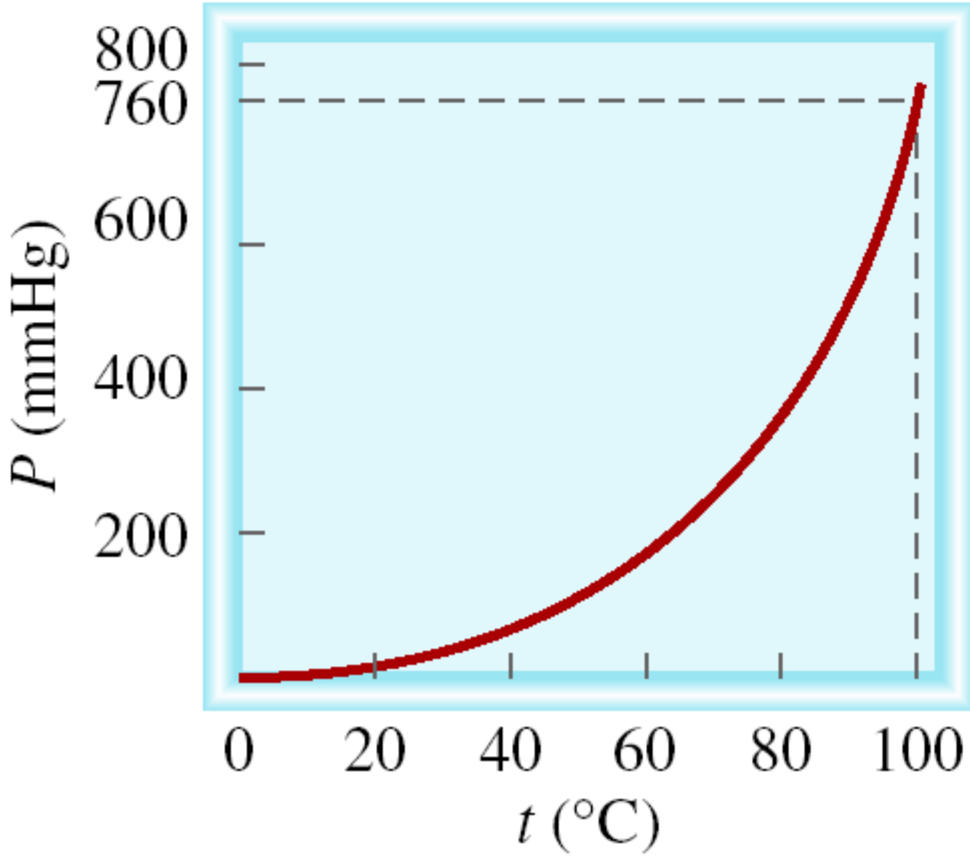


TABLE 5.3
Pressure of Water Vapor at Various Temperatures

Temperature (°C)	Water Vapor Pressure (mmHg)
0	4.58
5	6.54
10	9.21
15	12.79
20	17.54
25	23.76
30	31.82
35	42.18
40	55.32
45	71.88
50	92.51
55	118.04
60	149.38
65	187.54
70	233.7
75	289.1
80	355.1
85	433.6
90	525.76
95	633.90
100	760.00

Chemistry in Action:

Scuba Diving and the Gas Laws

Depth (ft)	Pressure (atm)
0	1
33	2
66	3

P $\downarrow$ V $\uparrow$

Kinetic Molecular Theory of Gases

1. A gas is composed of molecules that are separated from each other by distances far greater than their own dimensions. The molecules can be considered to be *points*; that is, they possess mass but have negligible volume.
2. Gas molecules are in constant motion in random directions, and they frequently collide with one another. Collisions among molecules are perfectly elastic.
3. Gas molecules exert neither attractive nor repulsive forces on one another.
4. The average kinetic energy of the molecules is proportional to the temperature of the gas in kelvins. Any two gases at the same temperature will have the same average kinetic energy

$$\overline{KE} = \frac{1}{2} m\overline{u^2}$$

Kinetic theory of gases and …

- Compressibility of Gases
- Boyle's Law

  $P \propto$ collision rate with wall

  Collision rate $\propto$ number density

  Number density $\propto 1/V$

  $P \propto 1/V$

- Charles' Law

  $P \propto$ collision rate with wall

  Collision rate $\propto$ average kinetic energy of gas molecules

  Average kinetic energy $\propto T$

  $P \propto T$

Kinetic theory of gases and …

- Avogadro's Law

  $P \alpha$ collision rate with wall

  Collision rate α number density

  Number density α n

  $P \alpha n$

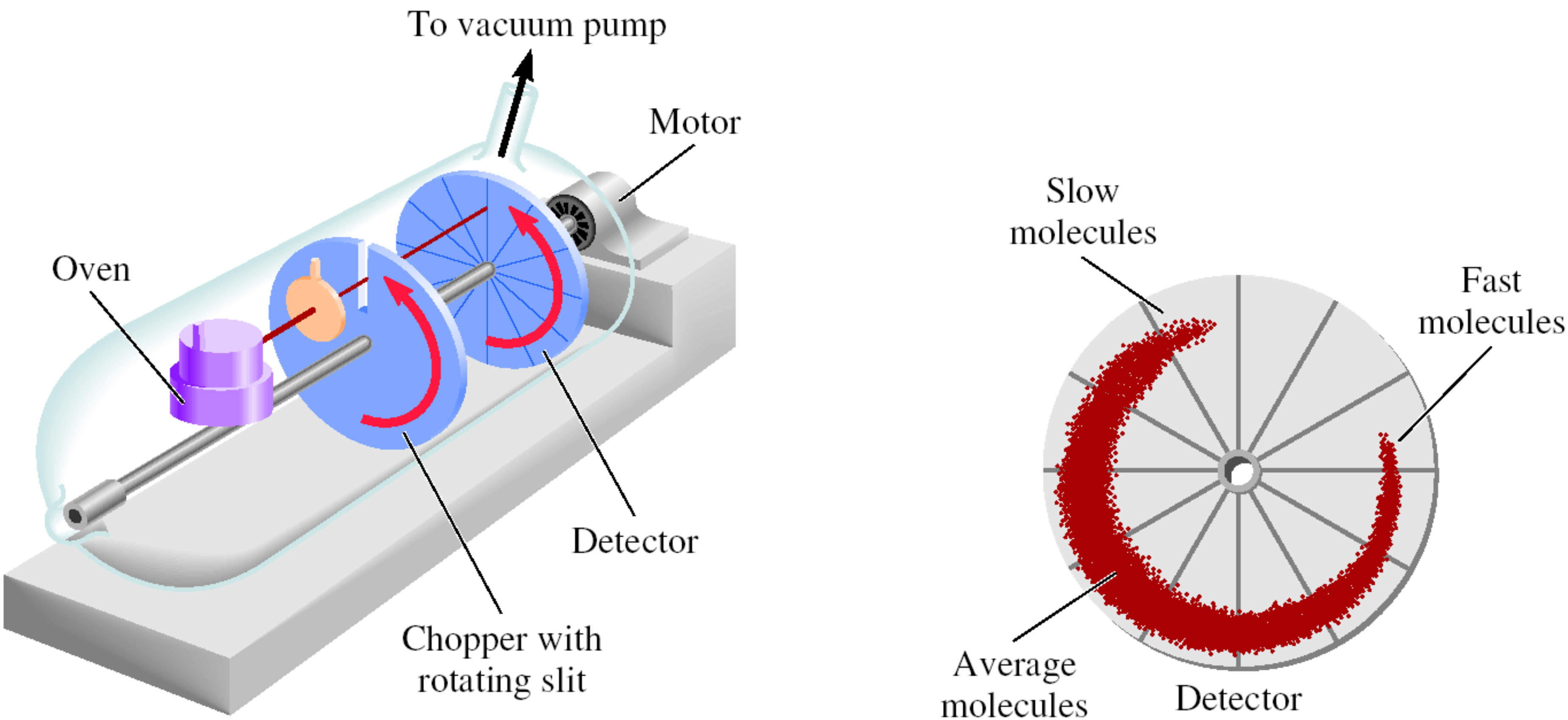
- Dalton's Law of Partial Pressures

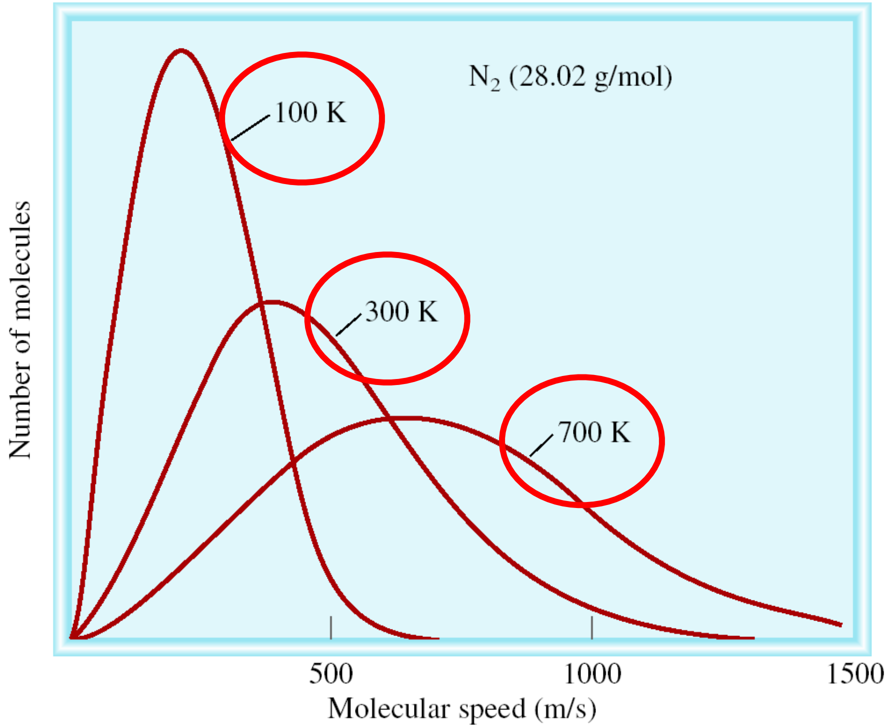
  Molecules do not attract or repel one another

  P exerted by one type of molecule is unaffected by the presence of another gas

  $P_{\text{total}} = \Sigma P_{\text{i}}$

Apparatus for Studying Molecular Speed Distributiona

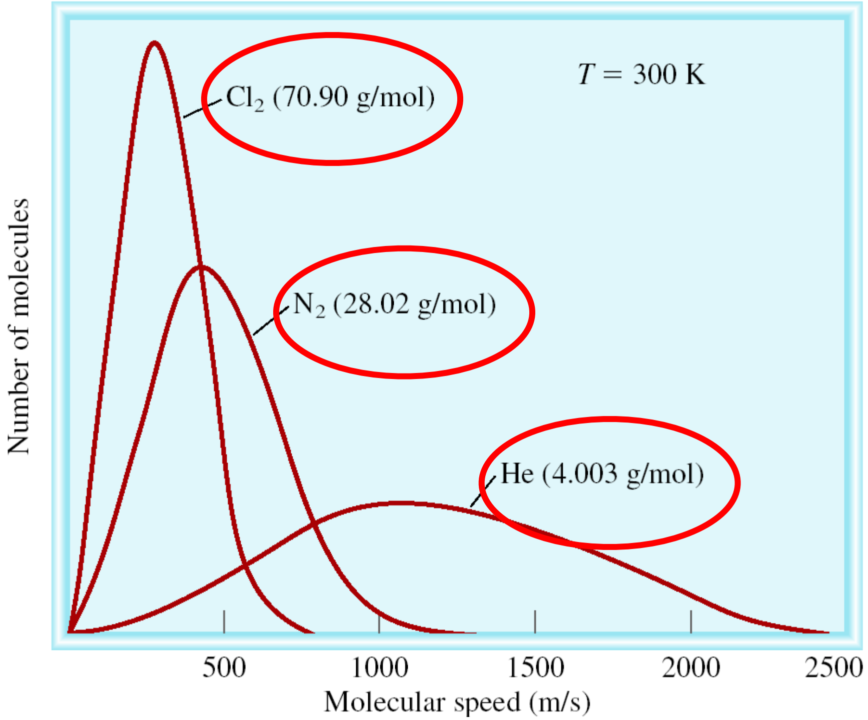




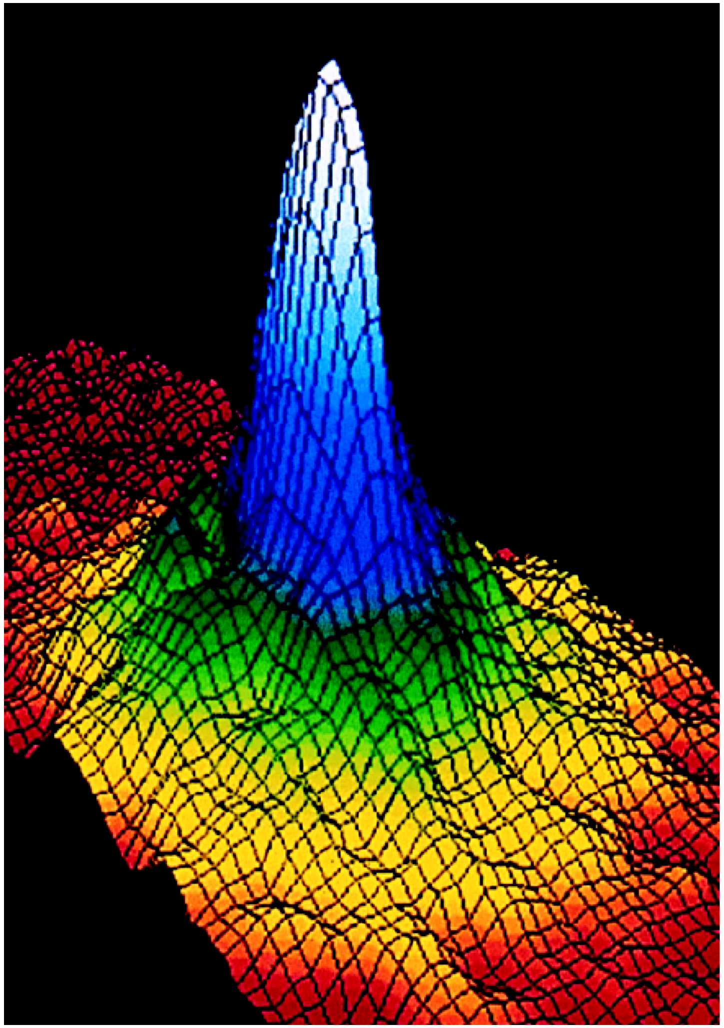
The distribution of speeds
of three different gases
at the same temperature

The distribution of speeds
for nitrogen gas molecules
at three different temperatures

$$u_{rms} = \sqrt{\frac{3RT}{M}}$$



Chemistry in Action: Super Cold Atoms



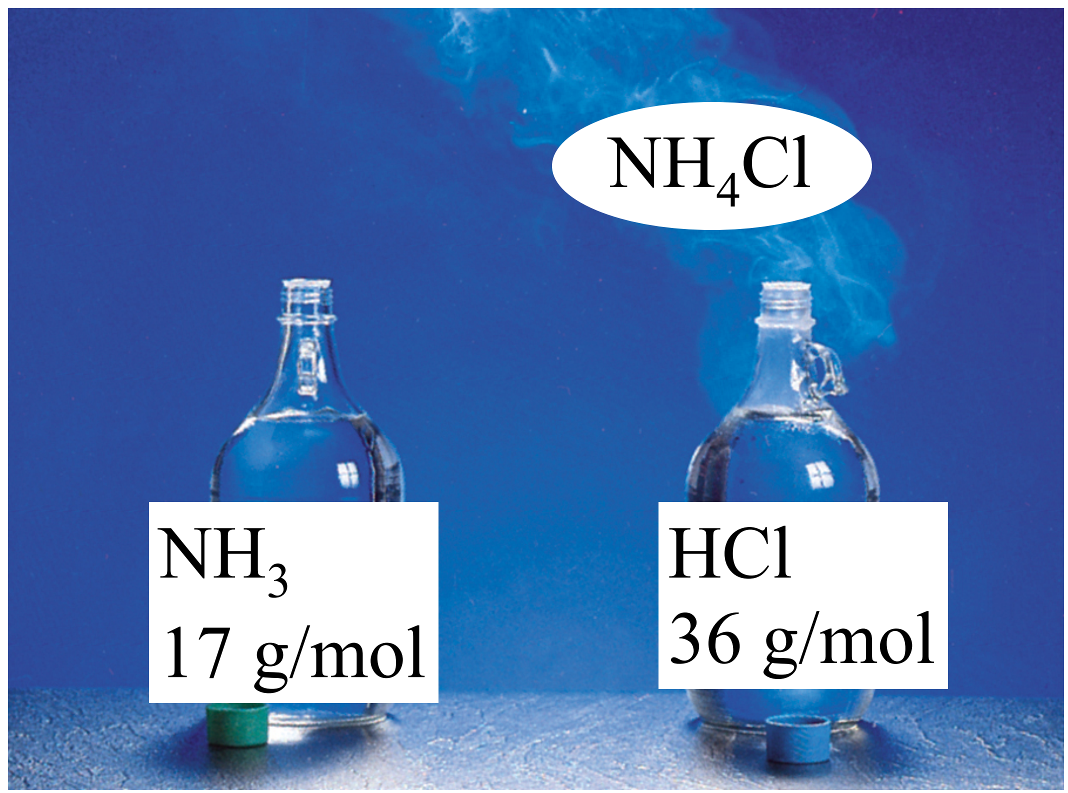
Maxwell velocity distribution of Rb atoms at about 1.7 x *10*$^{-7}$ *K*

Bose-Einstein condensate (*BEC*)

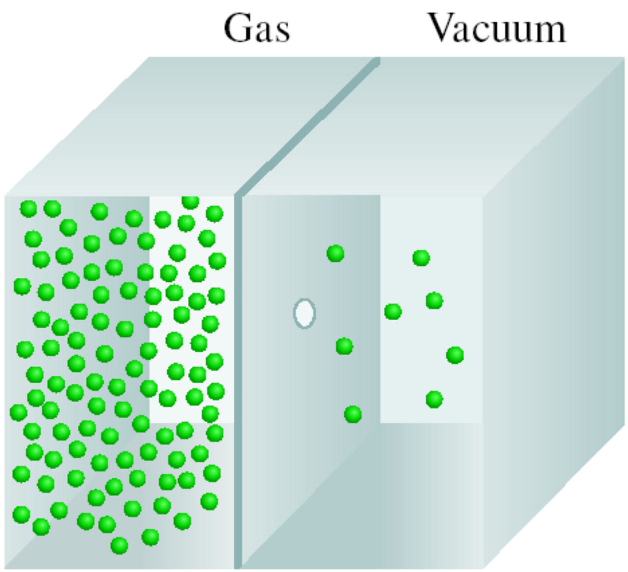
Gas diffusion is the gradual mixing of molecules of one gas with molecules of another by virtue of their kinetic properties.

molecular path

$$\frac{r_1}{r_2} = \sqrt{\frac{M_2}{M_1}}$$



Gas effusion is the is the process by which gas under pressure escapes from one compartment of a container to another by passing through a small opening.



$$\frac{r_1}{r_2} = \frac{t_2}{t_1} = \sqrt{\frac{M_2}{M_1}}$$

Nickel forms a gaseous compound of the formula $Ni(CO)_x$ What is the value of *x* given that under the same conditions methane (CH_4) effuses 3.3 times faster than the compound?

$r_1 = 3.3 \text{ x } r_2$

$$M_2 = \left(\frac{r_1}{r_2}\right)^2 \text{ x } M_1 = (3.3)^2 \text{ x } 16 = 174.2$$

$M_1 = 16$ g/mol

$58.7 + x \bullet 28 = 174.2$

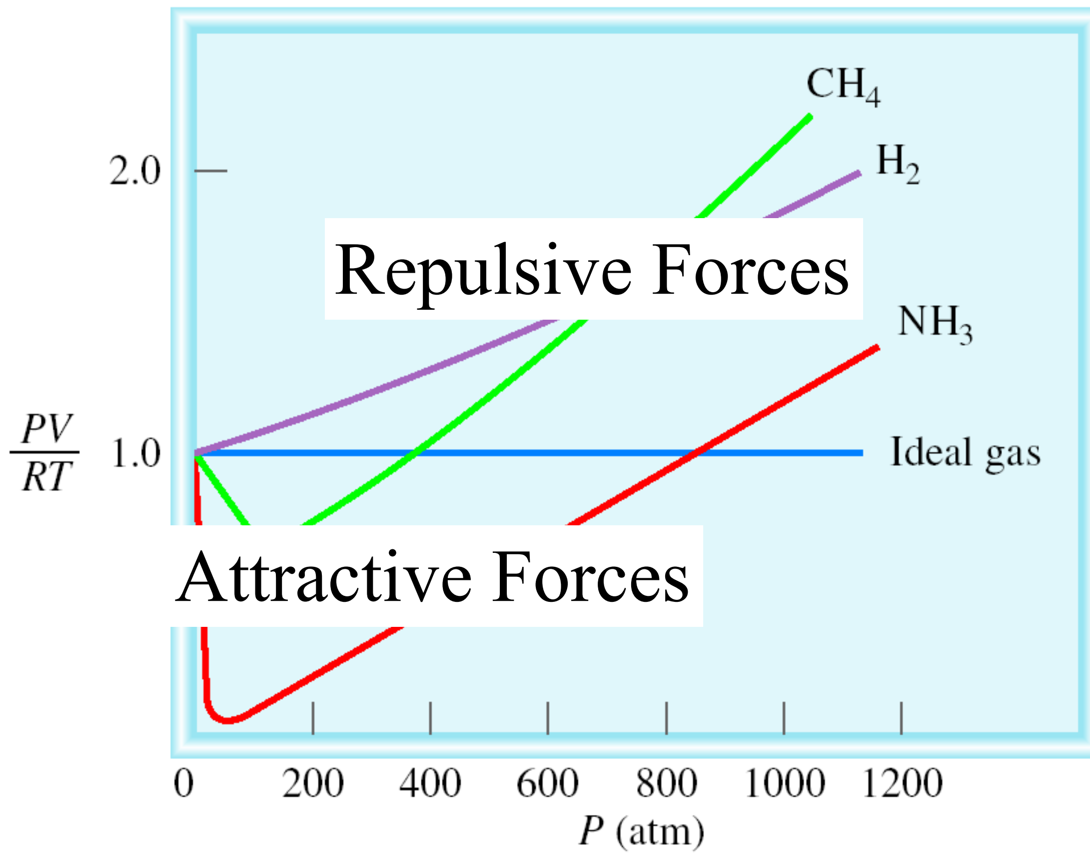
$x = 4.1 \sim 4$

Deviations from Ideal Behavior

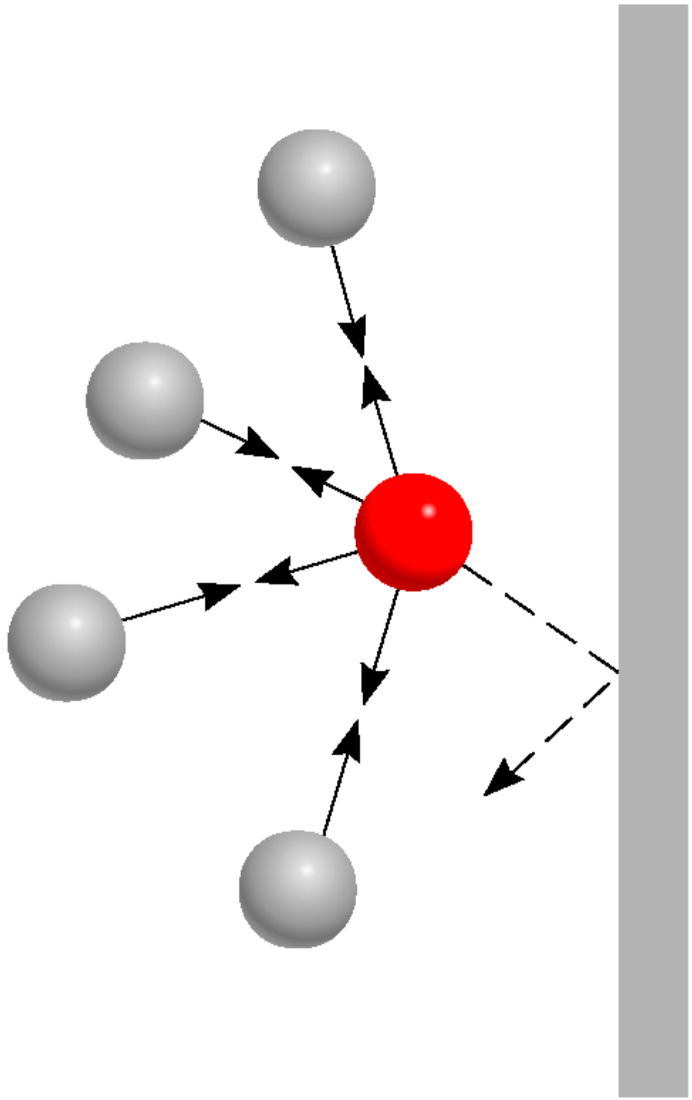
<u>1 mole of ideal gas</u>

$$PV = nRT$$

$$n = \frac{PV}{RT} = 1.0$$



Effect of intermolecular forces on the pressure exerted by a gas.



Van der Waals equation
nonideal gas

$$\underbrace{\left(P + \frac{an^2}{V^2}\right)}_{\text{corrected pressure}}\underbrace{(V - nb)}_{\text{corrected volume}} = nRT$$

TABLE 5.4

van der Waals Constants of Some Common Gases

Gas	a $\left(\frac{atm \cdot L^2}{mol^2}\right)$	b $\left(\frac{L}{mol}\right)$
He	0.034	0.0237
Ne	0.211	0.0171
Ar	1.34	0.0322
Kr	2.32	0.0398
Xe	4.19	0.0266
H_2	0.244	0.0266
N_2	1.39	0.0391
O_2	1.36	0.0318
Cl_2	6.49	0.0562
CO_2	3.59	0.0427
CH_4	2.25	0.0428
CCl_4	20.4	0.138
NH_3	4.17	0.0371
H_2O	5.46	0.0305