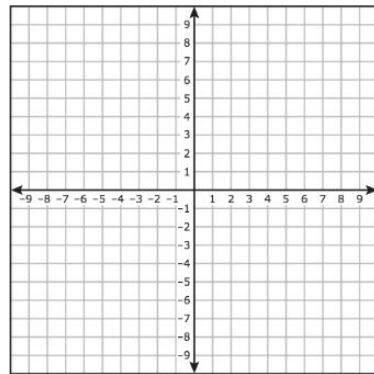


b) $2x^2 + 12x + 17$



4.) (20 pts total, 5 pts each) Factor each expression.

a) $x^2 + 5x - 14$

b) $x^2 + 7x + 12$

$\oplus \rightarrow \text{same sign}$
 $\ominus \rightarrow \text{different}$

c) $2x^2 - 13x + 15$

Factors of $2x^2$: $2x \cdot x$
 $(2x-3)(x-5)$

Factors of 15: $3 \cdot 5$ or $5 \cdot 3$
 $1 \cdot 15$ or $15 \cdot 1$

$-6x + (-5x) = -11x$

$-3x + (-10x) = -13x$

$2x - 5$

$2x - 3$

5

15

Larger Θ different

d) $3x^2 - 5x - 12$

factors $3x^2$: $3x \cdot x$
factors -12 : $2 \cdot -6$, $4 \cdot -3$, $1 \cdot -12$

$\begin{array}{|c|c|} \hline x & + \\ \hline 2 & | 6x - 12 \\ \hline \end{array}$

$\begin{array}{|c|c|} \hline 3x & -2 \\ \hline 3x & -2x \\ \hline 18x & -12 \\ \hline \end{array}$

$18x - 2x = 16x$

$\begin{array}{|c|c|} \hline x & + \\ \hline 3 & | -9x + 12 \\ \hline \end{array}$

$3x + 4$

$(3x+4)(x-3)$

$6x - 6x = 0$

5.) (10 pts total, 2.5 pts each) Evaluate the discriminant of the equation. Indicate the number of real roots for each.

Quadratic formula

a) $x^2 - 4x + 4$ 1 real

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$b^2 - 4ac = (-4)^2 - 4(1)(4)$$

$$16 - 16 = 0$$

b) $-2x^2 + 6x - 14$

a) -2 b) 6 c) -14

$$b^2 - 4ac = (6)^2 - 4(-2)(-14)$$

$$36 - 112 = -76$$

c) $x^2 + 9x + 18$ 0 reals

\oplus $b^2 - 4ac > 0$

\leftrightarrow 2 reals

\ominus $b^2 - 4ac = 0$

1 real

\ominus $b^2 - 4ac < 0$

0 reals

d) $2x^2 + 11x - 21$

6.) (15 pts total, 7.5 pts each) Solve using the Quadratic Equation.
Formula

a) $x^2 = 3x + 2$
 $-3x - 2$ $-3x - 2$

$$x^2 - 3x - 2 = 0$$

$a = 1 \quad b = -3 \quad c = -2$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$
$$\frac{-(-3) \pm \sqrt{(-3)^2 - 4(1)(-2)}}{2(1)}$$
$$\frac{3 \pm \sqrt{9 + 8}}{2} = \boxed{\frac{3 \pm \sqrt{17}}{2}}$$

b) $3x^2 - 5x = -12$

7.) (15 pts total, 7.5 pts each) Place each equation in vertex form by completing the square.
Please show all your work.

a) $x^2 = 5x + 14$

b) $(2x^2 + 6x) - 7 = 0$

- 1.) 2020 it
- 2.) Factor out a 2
- 3.) $(\frac{b}{2})^2$
- 4.) Square roots

$$2(x^2 + 3x) - 7 = 0$$

$$(\frac{3}{2})^2 = \frac{9}{4} \quad -\frac{9}{4}(2) = -\frac{18}{4} \quad -7 - \frac{18}{4}$$

$$2(x^2 + 3x + \frac{9}{4}) - 7 - \frac{18}{4} = 0 \quad -7 = \frac{-28}{4}$$

$$2(x^2 + 3x + \frac{9}{4}) - \frac{23}{2} = 0 \quad -\frac{28}{4} - \frac{18}{4} = -\frac{46}{4}$$

vertex form $2(x + \frac{3}{2})^2 - \frac{23}{2} = 0$ vertex: $(-\frac{3}{2}, -\frac{23}{2})$

- 8.) (20 pts total, 10 pts each) Graph each equation completely. Plot all roots, intercepts, and the vertex.

a) $(x^2 + 6x) + 9$

$$(\frac{b}{2})^2 + 9 \quad -9$$

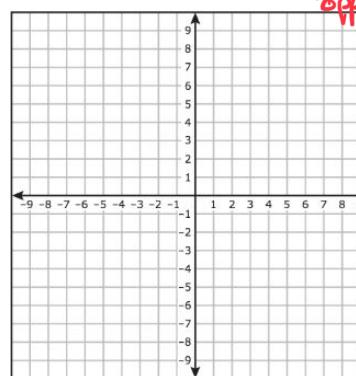
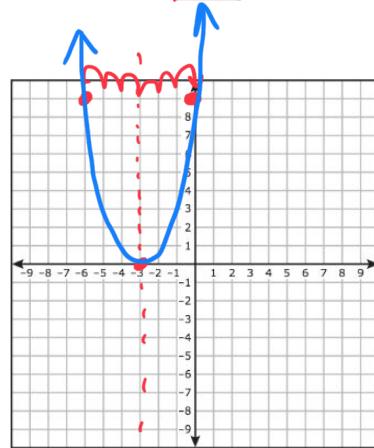
$$(\frac{6}{2})^2 \quad (x^2 + 6x + 9) + 9 - 9$$

$$3^2 = 9 \quad (x^2 + 6x + 9) + 0$$

$$\sqrt{x^2} \downarrow \quad \sqrt{9} \downarrow$$

$$(x + 3)^2 + 0 \quad \text{Vertex } (-3, 0)$$

$$(x + 3)^2 + 0 = 0 \quad \sqrt{(x + 3)^2} \sqrt{0} \quad x + 3 = 0 \quad x = -3$$



b) $x^2 - 4x - 5$

Vertex form: $a(x - h)^2 + k$
opp sign