

T-AZ Algebra 2

Week 26 3/19

4*4
2*8
1*16

$$\downarrow x^2 - 2x - 16 = 0$$

~~$$\begin{aligned} - & * & = -16 \\ - & + & = -2 \end{aligned}$$~~

Quadratic Formula

$a=1$ $b=-2$ $c=-16$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Simplify $\sqrt{68}$

$$\frac{-(-2) \pm \sqrt{(-2)^2 - 4(1)(-16)}}{2(1)}$$

Look for perfect squares

$$\frac{2 \pm \sqrt{4 + 64}}{2}$$

$$\begin{aligned} & \sqrt{68} \\ & \swarrow \searrow \\ & \sqrt{4} \cdot \sqrt{17} \\ & \downarrow \\ & 2\sqrt{17} \end{aligned}$$

$$\frac{2 \pm \sqrt{68}}{2} = \frac{2 \pm 2\sqrt{17}}{2}$$

+3 +5 +7 +9 +11 +13 +15 +17 +19 +21
1, 4, 9, 16, 25, 36, 49, 64, 81, 100, 121

$$\boxed{1 \pm \sqrt{17}}$$

$$\boxed{1 + \sqrt{17}, 1 - \sqrt{17}}$$

$$x^2 - 2x - 16 = 0$$

Find vertex

$$h = \frac{-b}{2a} = \frac{-(-2)}{2(1)} = \frac{2}{2} = 1$$

vertex: $(1, -17)$

$$x^2 - 2x - 16 =$$

$$(1)^2 - 2(1) - 16$$

$$1 - 2 - 16 = -1 - 16 = -17$$

or...

take the average of the zeros

Quadratic Formula

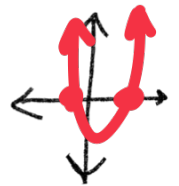
$$\frac{1 \pm \sqrt{17} + 1 \mp \sqrt{17}}{2} + \frac{2}{2}$$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \text{ — discriminant } \textcircled{1}$$

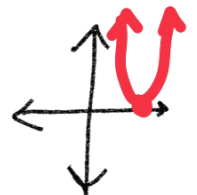
$$y = ax^{\textcircled{2}} + bx + c$$

of zeros possible

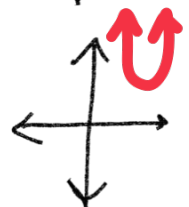
if..... $b^2 - 4ac > 0 \rightarrow 2 \text{ zeros}$



\oplus
 $b^2 - 4ac = 0 \rightarrow 1 \text{ zero}$



\ominus
 $b^2 - 4ac < 0 \rightarrow 0 \text{ zeros}$



$$x^2 + 4x - 18 = 0$$

Find zero(s).

Use discriminant to confirm # of zeros

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$a = 1 \quad b = 4 \quad c = -18$$

$$\frac{-4 \pm \sqrt{(4)^2 - 4(1)(-18)}}{2(1)}$$

$$\frac{-4 \pm \sqrt{16 + 72}}{2}$$

$$\frac{-4 \pm \sqrt{88}}{2}$$

According to discriminant,
2 zeros

$$\frac{-2 \pm 2\sqrt{22}}{2}$$

$$\boxed{-2 \pm \sqrt{22}}$$

$$\begin{array}{c} \sqrt{88} \\ \wedge \\ \sqrt{4} \quad \sqrt{22} \\ \downarrow \\ 2\sqrt{22} \end{array}$$

$$-2 + \sqrt{22} \text{ and } -2 - \sqrt{22}$$

$$x^2 + 4x + 12 = 0$$

$$a = 1 \quad b = 4 \quad c = 12$$

$$\sqrt{-32} = \sqrt{-1} \cdot \sqrt{32}$$

$$\begin{array}{l} \downarrow \\ i \cdot \sqrt{16} \cdot \sqrt{2} \\ 4i\sqrt{2} \end{array}$$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\frac{-4 \pm \sqrt{(4)^2 - 4(1)(12)}}{2(1)}$$

∅ zeros

$$\frac{-4 \pm \sqrt{16 - 48}}{2} = \frac{-4 \pm \sqrt{-32}}{2}$$

$$\frac{-2 \pm 2i\sqrt{2}}{2} \quad \boxed{-2 \pm 2i\sqrt{2}} \quad \sqrt{-1} = i$$

$$3x^2 + 2x + 8 = 0$$

\downarrow \downarrow \downarrow
 $a=3$ $b=2$ $c=8$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\frac{-2 \pm \sqrt{(2)^2 - 4(3)(8)}}{2(3)}$$

$$\frac{-2 \pm \sqrt{4 - 96}}{6}$$

$$\frac{-2 \pm \sqrt{-92}}{6}$$

$$\frac{-2 \pm 2i\sqrt{23}}{6}$$

$$\boxed{\frac{-1 \pm i\sqrt{23}}{3}}$$

Discriminant
 $-92 \rightarrow \emptyset$ zeros

h term in the vertex
 $-\frac{2}{6} = -\frac{1}{3}$

$$\sqrt{-92} = \sqrt{-1} \cdot \sqrt{92}$$

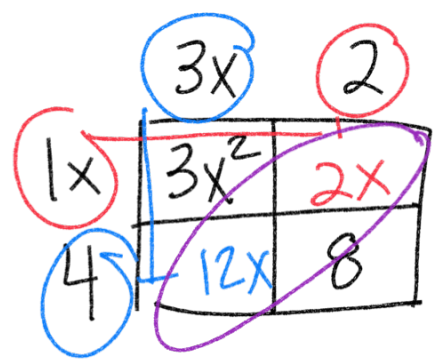
$$i\sqrt{92}$$

$$i \cdot \sqrt{4} \cdot \sqrt{23}$$

$$2i\sqrt{23}$$

$$3x^2 + 2x + 8$$

\uparrow \uparrow
 $3 \cdot 1$ $8 \cdot 1$
 $4 \cdot 2$



$$12x + 2x = 14x$$

