

S-G Geometry Session 6 6/27

Given: $4x + 3 = 27$

Prove: $x = 6$

Statements

$$4x + 3 = 27$$

$$\begin{array}{r} -3 \quad -3 \end{array}$$

$$\frac{4x}{4} = \frac{24}{4}$$

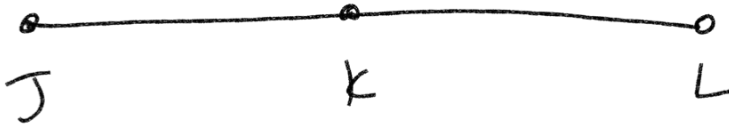
$$x = 6$$

Reasons

Given

subtraction P.o.E

Division P.o.E



Given:

$$\overline{JK} = 5x$$

$$\overline{JL} = 62$$

$$\overline{KL} = 8x - 3$$

Prove:

$$x = 5$$

Statement

$$\overline{JK} = 5x$$

$$\overline{JL} = 62$$

$$\overline{KL} = 8x - 3$$



Reason

Given

Segment Addition Postulate (SAP)

Substitution

Simplify

Add P.o.E

Division P.o.E

$$\overline{JK} + \overline{KL} = \overline{JL}$$

$$\begin{array}{ccc} \downarrow & \downarrow & \downarrow \end{array}$$

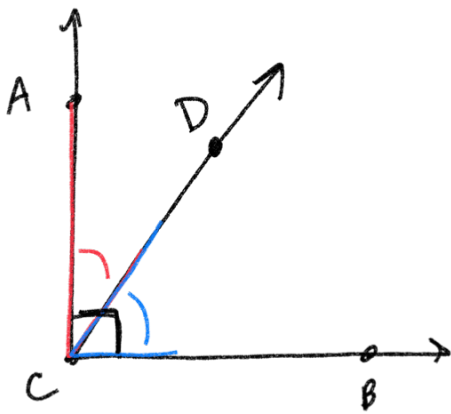
$$5x + 8x - 3 = 62$$

$$13x - 3 = 62$$

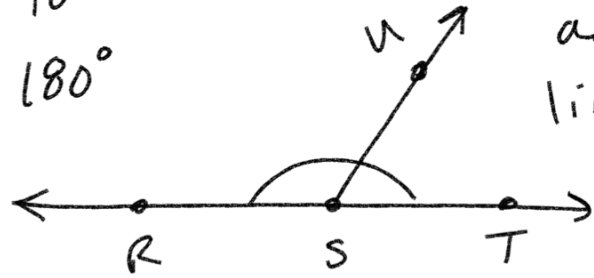
$$\begin{array}{cc} +3 & +3 \end{array}$$

$$\frac{13x}{13} = \frac{65}{13}$$

$$x = 5$$



$C \rightarrow 90^\circ$
 $S \rightarrow 180^\circ$



Because adjacent, linear pair.

$\angle RST = 180^\circ$
 straight line

$\angle RSU + \angle UST = 180^\circ$
 Angle Addition Postulate
 $\angle RSU$ & $\angle UST$ are
 supplemental angles

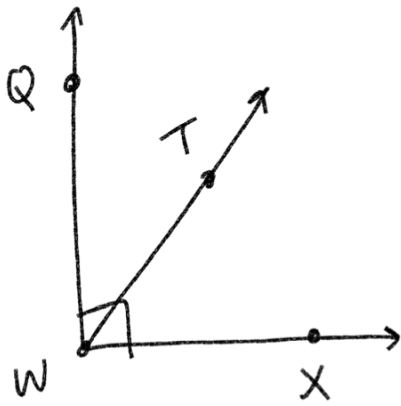
$\angle ACB = 90^\circ$

Right Angle
Perpendicular

$\angle ACD + \angle DCB = 90^\circ$

Angle Addition Postulate

$\angle ACD$ & $\angle DCB$ are
complementary angles



Given $\angle QWT = 2x$

$\angle TWX = x + 6$

$\angle QWX$ is right angle

Prove: $x = 28$

Statements

$\angle QWT = 2x$

$\angle TWX = x + 6$

$\angle QWX$ is right angle

$\angle QWX = 90^\circ$

$\angle QWT + \angle TWX = \angle QWX$

$2x + x + 6 = 90^\circ$

$3x + 6 = 90$

$\quad -6 \quad -6$

$\frac{3x}{3} = \frac{84}{3}$

$x = 28$

Reasons

} Given

Definition of Right Angle

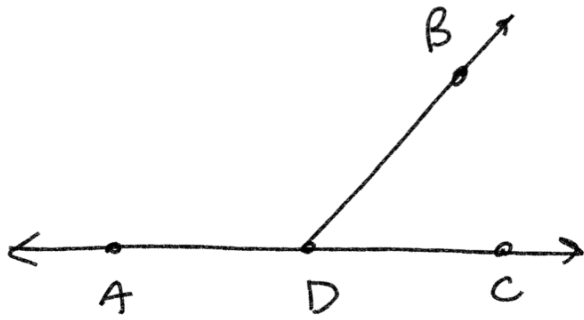
Angle Addition Postulate (AAP)

substitution

simplify

Subtract PoE

Division PoE



Given: $\angle ADB = 3x + 6$

$\angle BDC = 2x + 4$

Prove: $x = 34$

Statements

$\angle ADB = 3x + 6$

$\angle BDC = 2x + 4$

$\angle ADC = 180^\circ$

$\rightarrow \angle ADB + \angle BDC = 180^\circ$
or

$\rightarrow \angle ADB + \angle BDC = \angle ADC$

$3x + 6 + 2x + 4 = 180^\circ$

$5x + 10 = 180^\circ$
-10 -10

$\{ 5x = 170$
 $\{ \frac{5x}{5} = \frac{170}{5}$

$x = 34$

Reasons

Given

Definition of a line

Definition of supplemental angles.

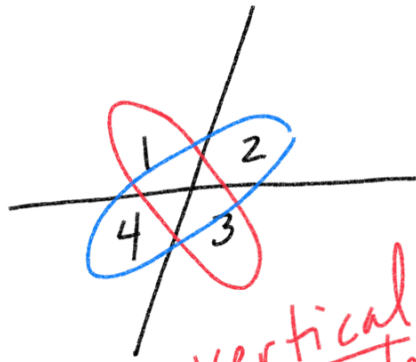
Angle Add Postulate

substitution

simplify

subtract PoE

Divide PoE



vertical angles



Statement

$$\angle 1 + \angle 2 = 180^\circ$$

$$\angle 2 + \angle 3 = 180^\circ$$

$$\begin{aligned} \angle 1 + \angle 2 &= \angle 2 + \angle 3 \\ -\angle 2 & \quad -\angle 2 \end{aligned}$$

$$\angle 1 = \angle 3$$

$$\angle 1 \cong \angle 3$$

Reason

supplemental
or
Linear pair

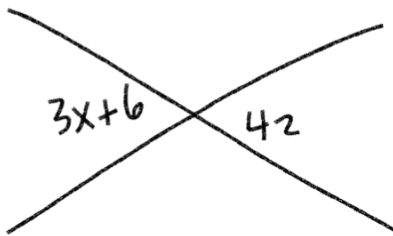
linear pairs

substitution
or

sylogism/transitive
property

Subtract PoE

Definition of
congruency



Prove: $x = 12$

statement

$$\begin{aligned} 3x + 6 &= 42 \\ -6 & \quad -6 \end{aligned}$$

$$\begin{aligned} 3x &= 36 \\ \frac{3}{3} & \quad \frac{3}{3} \end{aligned}$$

$$x = 12$$

Reasons

Vertical Angles

Subtract PoE

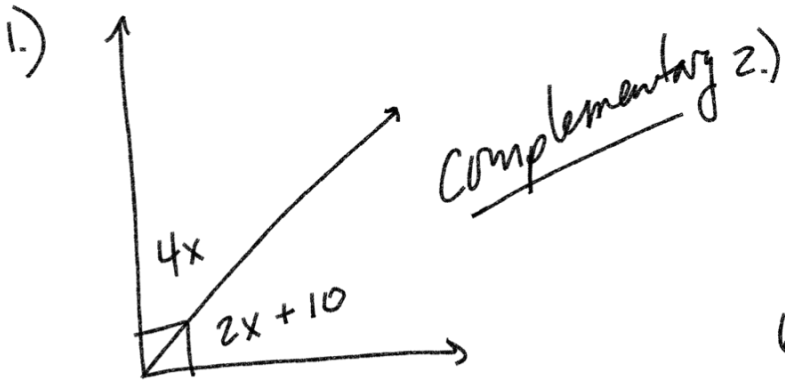
Division PoE

Complementary

Supplementary/Linear Pair

Vertical Angles

SAP/AAP



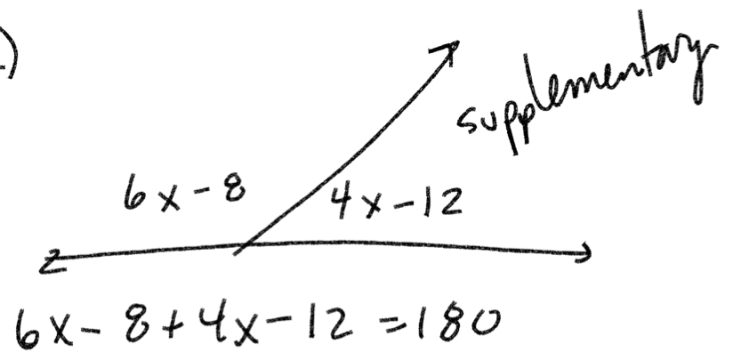
Not drawn to scale.

$$4x + 2x + 10 = 90$$

$$\begin{array}{r} 6x + 10 = 90 \\ -10 \quad -10 \end{array}$$

$$\frac{6x}{6} = \frac{80}{6}$$

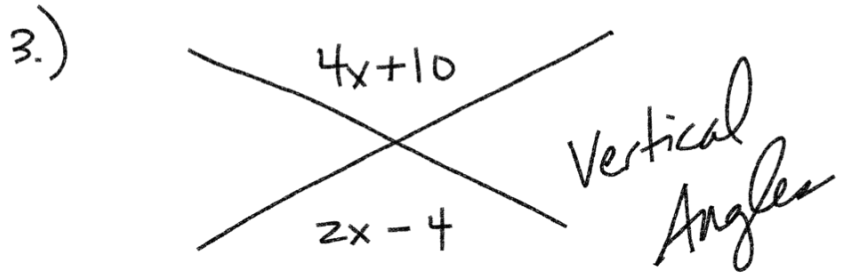
$$\boxed{x = 13.\bar{3}}$$



$$6x - 8 + 4x - 12 = 180$$

$$\begin{array}{r} 10x - 20 = 180 \\ +20 \quad +20 \end{array}$$

$$\frac{10x}{10} = \frac{200}{10} \quad \boxed{x = 20}$$



$$\begin{array}{r} 4x + 10 = 2x - 4 \\ -2x \quad -2x \end{array}$$

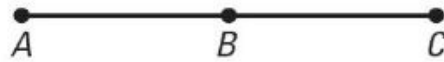
$$\begin{array}{r} 2x + 10 = -4 \\ -10 \quad -10 \end{array}$$

$$\frac{2x}{2} = \frac{-14}{2}$$

$$\boxed{x = -7}$$

Geometry Proof Supplemental

- 1.) Given: $AC = AB + AB$
 Prove: $AB = BC$



Statement

$\rightarrow AB + AB = AC$

$AB + BC = AC$

$AB + BC = AB + AB$

$\swarrow -AB \quad \swarrow -AB$

$BC = AB$

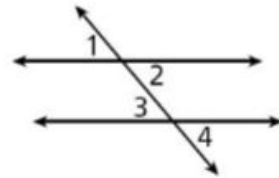
Reason

Given

Angle Addition Post

substitution or Syllogism/
 subtract P o E Transitive Property

- 2.) Given: $\angle 1 \cong \angle 4$
 Prove: $\angle 2 \cong \angle 3$



Statement

$\angle 1 \cong \angle 2$

$\angle 3 \cong \angle 4$

$\angle 1 \cong \angle 4$

$\angle 2 \cong \angle 3$

Reason

vertical angles

vertical angles

given

substitute

$\angle 1 = \angle 2$

$\angle 3 = \angle 4$

$\angle 1 = \angle 4$

$\angle 1 = \angle 2$

$\angle 3 = \angle 4$

$\angle 1 = \angle 4$

$\angle 2 = \angle 3$