

## Assignment

Date \_\_\_\_\_ Period \_\_\_\_\_

**For each function, identify the holes, horizontal asymptote, and domain.**

1)  $f(x) = \frac{x^3 + x^2 - 2x}{-4x^2 - 12x}$

2)  $f(x) = \frac{x^3 - x^2 - 6x}{3x^2 - 3x - 6}$

3)  $f(x) = \frac{x + 1}{x^2 + 3x}$

4)  $f(x) = \frac{x^2 + 4x}{-4x^2 - 8x + 12}$

5)  $f(x) = \frac{-x^2 + 16}{x^2 + 2x - 8}$

6)  $f(x) = \frac{x^2 - 9}{-3x - 3}$

7)  $f(x) = \frac{x^3 - 9x}{-4x^2 - 16x}$

8)  $f(x) = \frac{1}{4x + 8}$

9)  $f(x) = \frac{x^2 + x - 12}{4x + 12}$

10)  $f(x) = \frac{x^3 - 4x}{-4x^2 - 12x}$

$$11) \ f(x) = \frac{2x^2 - 2}{x^2 - 4}$$

$$12) \ f(x) = -\frac{3}{x - 4}$$

$$13) \ f(x) = \frac{-3x - 3}{x^2 + 4x + 3}$$

$$14) \ f(x) = \frac{-2x^3 - 6x^2 - 4x}{x^3 - 4x}$$

$$15) \ f(x) = \frac{-2x - 6}{x - 1}$$

$$16) \ f(x) = \frac{x + 4}{2x + 4}$$

$$17) \ f(x) = \frac{x^2 - x}{4x - 12}$$

$$18) \ f(x) = \frac{x - 4}{-2x}$$

$$19) \ f(x) = \frac{x^2 - 9}{-4x}$$

$$20) \ f(x) = \frac{x^2 - 5x + 6}{2x^2 + 6x}$$

$$21) \ f(x) = \frac{x^3 + x^2 - 12x}{3x^2 - 3x}$$

$$22) \ f(x) = \frac{x^3 - 16x}{-4x^2 - 4x + 8}$$

$$23) \ f(x) = \frac{x^2 - 2x - 3}{3x - 12}$$

$$24) \ f(x) = -\frac{2}{x + 1}$$

$$25) \ f(x) = \frac{x^2 + 3x}{4x + 4}$$

$$26) \ f(x) = \frac{4}{x - 2}$$

$$27) \ f(x) = \frac{x^2 + 3x - 4}{3x^2 - 3x}$$

$$28) \ f(x) = \frac{x^3 - x^2 - 12x}{-4x^2 + 4x + 8}$$

$$29) \ f(x) = \frac{-2x^3 - 2x^2}{x^3 - 3x^2 - 4x}$$

$$30) \ f(x) = \frac{-x^2 + 3x}{x^2 - x}$$

$$31) \ f(x) = \frac{x^2 - x}{-4x - 8}$$

$$32) \ f(x) = \frac{4}{x^2 + x - 6}$$

$$33) \ f(x) = -\frac{3}{x^2 - 4}$$

$$34) \ f(x) = \frac{-3x^2 + 21x - 36}{x^2 - 5x + 4}$$

$$35) \ f(x) = \frac{2x^2 + 12x + 16}{x^2 + x - 6}$$

$$36) \ f(x) = \frac{1}{-2x + 4}$$

$$37) \ f(x) = \frac{2x^2 - 4x - 16}{x^2 - 3x - 4}$$

$$38) \ f(x) = \frac{3}{x + 2}$$

$$39) \ f(x) = \frac{x^2 - x - 12}{4x + 8}$$

$$40) \ f(x) = \frac{x^2 + x - 2}{-3x - 9}$$

$$41) \ f(x) = \frac{x + 4}{-2x^2 + 2x + 4}$$

$$42) \ f(x) = \frac{-2x^2 + 18}{x^2 - 5x + 6}$$

$$43) \ f(x) = \frac{1}{-3x^2 + 12}$$

$$44) \ f(x) = \frac{1}{3x - 12}$$

$$45) \ f(x) = \frac{1}{-x}$$

$$46) \ f(x) = \frac{x - 4}{-x - 3}$$

$$47) \ f(x) = \frac{-2x^3 + 4x^2}{x^3 - 6x^2 + 8x}$$

$$48) \ f(x) = \frac{x^2 + 4x + 3}{-4x + 4}$$

$$49) \ f(x) = \frac{x}{x + 3}$$

$$50) \ f(x) = \frac{x^3 + 5x^2 + 4x}{3x^2 + 6x - 9}$$

$$51) \ f(x) = \frac{x^2 + 5x + 6}{3x^2 - 3x - 6}$$

$$52) \ f(x) = \frac{x^2 + 3x}{-4x^2 + 4x + 48}$$

$$53) \ f(x) = \frac{-3x^2 + 6x}{x^2 - 2x - 3}$$

$$54) \ f(x) = \frac{x}{-3x^2 - 9x}$$

$$55) \ f(x) = \frac{x^2 + x}{4x + 12}$$

$$56) \ f(x) = \frac{-x^2 - x}{x^2 + x - 6}$$

$$57) \ f(x) = \frac{2}{x^2 - x - 2}$$

$$58) \ f(x) = \frac{x^3 + 3x^2 + 2x}{-3x^2 - 9x}$$

$$59) \ f(x) = \frac{x^2 - 9}{-x^2 + 5x - 6}$$

$$60) \ f(x) = \frac{-x - 3}{x^2 + 4x + 3}$$

$$61) \ f(x) = \frac{-x^2 + 5x - 6}{x^2 + 2x - 3}$$

$$62) \ f(x) = \frac{1}{x^2 - 2x - 3}$$

$$63) \ f(x) = \frac{x^2 + 2x - 3}{4x^2 + 12x}$$

$$64) \ f(x) = \frac{x + 1}{x - 3}$$

$$65) \ f(x) = \frac{x + 4}{3x - 12}$$

$$66) \ f(x) = \frac{-3x - 9}{x^2 + 5x + 6}$$

$$67) \ f(x) = -\frac{2}{x^2 + 3x}$$

$$68) \ f(x) = \frac{2x^2 + 10x + 8}{x^2 - 1}$$

$$69) \ f(x) = \frac{-x^2 - x}{x^2 + x - 2}$$

$$70) \ f(x) = \frac{x^3 - 7x^2 + 12x}{-4x^2 + 12x + 16}$$

$$71) \ f(x) = \frac{x^3 + 2x^2 - 8x}{-4x^2 + 12x}$$

$$72) \ f(x) = \frac{3x - 9}{x^3 - 5x^2 + 6x}$$

$$73) \ f(x) = \frac{x^2 + 4x}{-2x^2 - 4x + 6}$$

$$74) \ f(x) = \frac{1}{x^2 + x - 6}$$

$$75) \ f(x) = \frac{x^2 - 4x}{4x - 8}$$

$$76) \ f(x) = \frac{x^2 - 4x}{-4x - 4}$$

$$77) \ f(x) = \frac{x^3 + 2x^2 - 3x}{4x^2 + 20x + 24}$$

$$78) \ f(x) = \frac{1}{x + 2}$$

$$79) \ f(x) = \frac{x^3 - 6x^2 + 8x}{4x^2 - 12x}$$

$$80) \ f(x) = \frac{x^2 + 3x + 2}{-3x - 12}$$

## Assignment

Date \_\_\_\_\_ Period \_\_\_\_\_

**For each function, identify the holes, horizontal asymptote, and domain.**

$$1) \ f(x) = \frac{x^3 + x^2 - 2x}{-4x^2 - 12x}$$

Holes:  $x = 0$   
 Horz. Asym.: None  
 Domain: All reals except  $-3, 0$

$$2) \ f(x) = \frac{x^3 - x^2 - 6x}{3x^2 - 3x - 6}$$

Holes: None  
 Horz. Asym.: None  
 Domain: All reals except  $-1, 2$

$$3) \ f(x) = \frac{x + 1}{x^2 + 3x}$$

Holes: None  
 Horz. Asym.:  $y = 0$   
 Domain: All reals except  $-3, 0$

$$4) \ f(x) = \frac{x^2 + 4x}{-4x^2 - 8x + 12}$$

Holes: None  
 Horz. Asym.:  $y = -\frac{1}{4}$   
 Domain: All reals except  $-3, 1$

$$5) \ f(x) = \frac{-x^2 + 16}{x^2 + 2x - 8}$$

Holes:  $x = -4$   
 Horz. Asym.:  $y = -1$   
 Domain: All reals except  $-4, 2$

$$6) \ f(x) = \frac{x^2 - 9}{-3x - 3}$$

Holes: None  
 Horz. Asym.: None  
 Domain: All reals except  $-1$

$$7) \ f(x) = \frac{x^3 - 9x}{-4x^2 - 16x}$$

Holes:  $x = 0$   
 Horz. Asym.: None  
 Domain: All reals except  $-4, 0$

$$8) \ f(x) = \frac{1}{4x + 8}$$

Holes: None  
 Horz. Asym.:  $y = 0$   
 Domain: All reals except  $-2$

$$9) \ f(x) = \frac{x^2 + x - 12}{4x + 12}$$

Holes: None  
 Horz. Asym.: None  
 Domain: All reals except  $-3$

$$10) \ f(x) = \frac{x^3 - 4x}{-4x^2 - 12x}$$

Holes:  $x = 0$   
 Horz. Asym.: None  
 Domain: All reals except  $-3, 0$

$$11) \ f(x) = \frac{2x^2 - 2}{x^2 - 4}$$

Holes: None  
Horz. Asym.:  $y = 2$   
Domain: All reals except  $-2, 2$

$$12) \ f(x) = -\frac{3}{x - 4}$$

Holes: None  
Horz. Asym.:  $y = 0$   
Domain: All reals except  $4$

$$13) \ f(x) = \frac{-3x - 3}{x^2 + 4x + 3}$$

Holes:  $x = -1$   
Horz. Asym.:  $y = 0$   
Domain: All reals except  $-3, -1$

$$14) \ f(x) = \frac{-2x^3 - 6x^2 - 4x}{x^3 - 4x}$$

Holes:  $x = -2, x = 0$   
Horz. Asym.:  $y = -2$   
Domain: All reals except  $-2, 0, 2$

$$15) \ f(x) = \frac{-2x - 6}{x - 1}$$

Holes: None  
Horz. Asym.:  $y = -2$   
Domain: All reals except  $1$

$$16) \ f(x) = \frac{x + 4}{2x + 4}$$

Holes: None  
Horz. Asym.:  $y = \frac{1}{2}$   
Domain: All reals except  $-2$

$$17) \ f(x) = \frac{x^2 - x}{4x - 12}$$

Holes: None  
Horz. Asym.: None  
Domain: All reals except  $3$

$$18) \ f(x) = \frac{x - 4}{-2x}$$

Holes: None  
Horz. Asym.:  $y = -\frac{1}{2}$   
Domain: All reals except  $0$

$$19) \ f(x) = \frac{x^2 - 9}{-4x}$$

Holes: None  
Horz. Asym.: None  
Domain: All reals except  $0$

$$20) \ f(x) = \frac{x^2 - 5x + 6}{2x^2 + 6x}$$

Holes: None  
Horz. Asym.:  $y = \frac{1}{2}$   
Domain: All reals except  $-3, 0$

$$21) \ f(x) = \frac{x^3 + x^2 - 12x}{3x^2 - 3x}$$

Holes:  $x = 0$   
Horz. Asym.: None  
Domain: All reals except  $0, 1$

$$22) \ f(x) = \frac{x^3 - 16x}{-4x^2 - 4x + 8}$$

Holes: None  
Horz. Asym.: None  
Domain: All reals except  $-2, 1$

$$23) \ f(x) = \frac{x^2 - 2x - 3}{3x - 12}$$

Holes: None  
Horz. Asym.: None  
Domain: All reals except 4

$$24) \ f(x) = -\frac{2}{x + 1}$$

Holes: None  
Horz. Asym.:  $y = 0$   
Domain: All reals except -1

$$25) \ f(x) = \frac{x^2 + 3x}{4x + 4}$$

Holes: None  
Horz. Asym.: None  
Domain: All reals except -1

$$26) \ f(x) = \frac{4}{x - 2}$$

Holes: None  
Horz. Asym.:  $y = 0$   
Domain: All reals except 2

$$27) \ f(x) = \frac{x^2 + 3x - 4}{3x^2 - 3x}$$

Holes:  $x = 1$   
Horz. Asym.:  $y = \frac{1}{3}$   
Domain: All reals except 0, 1

$$28) \ f(x) = \frac{x^3 - x^2 - 12x}{-4x^2 + 4x + 8}$$

Holes: None  
Horz. Asym.: None  
Domain: All reals except -1, 2

$$29) \ f(x) = \frac{-2x^3 - 2x^2}{x^3 - 3x^2 - 4x}$$

Holes:  $x = -1, x = 0$   
Horz. Asym.:  $y = -2$   
Domain: All reals except -1, 0, 4

$$30) \ f(x) = \frac{-x^2 + 3x}{x^2 - x}$$

Holes:  $x = 0$   
Horz. Asym.:  $y = -1$   
Domain: All reals except 0, 1

$$31) \ f(x) = \frac{x^2 - x}{-4x - 8}$$

Holes: None  
Horz. Asym.: None  
Domain: All reals except -2

$$32) \ f(x) = \frac{4}{x^2 + x - 6}$$

Holes: None  
Horz. Asym.:  $y = 0$   
Domain: All reals except -3, 2

$$33) \ f(x) = -\frac{3}{x^2 - 4}$$

Holes: None  
Horz. Asym.:  $y = 0$   
Domain: All reals except -2, 2

$$34) \ f(x) = \frac{-3x^2 + 21x - 36}{x^2 - 5x + 4}$$

Holes:  $x = 4$   
Horz. Asym.:  $y = -3$   
Domain: All reals except 1, 4

$$35) \ f(x) = \frac{2x^2 + 12x + 16}{x^2 + x - 6}$$

Holes: None  
Horz. Asym.:  $y = 2$   
Domain: All reals except  $-3, 2$

$$36) \ f(x) = \frac{1}{-2x + 4}$$

Holes: None  
Horz. Asym.:  $y = 0$   
Domain: All reals except  $2$

$$37) \ f(x) = \frac{2x^2 - 4x - 16}{x^2 - 3x - 4}$$

Holes:  $x = 4$   
Horz. Asym.:  $y = 2$   
Domain: All reals except  $-1, 4$

$$38) \ f(x) = \frac{3}{x + 2}$$

Holes: None  
Horz. Asym.:  $y = 0$   
Domain: All reals except  $-2$

$$39) \ f(x) = \frac{x^2 - x - 12}{4x + 8}$$

Holes: None  
Horz. Asym.: None  
Domain: All reals except  $-2$

$$40) \ f(x) = \frac{x^2 + x - 2}{-3x - 9}$$

Holes: None  
Horz. Asym.: None  
Domain: All reals except  $-3$

$$41) \ f(x) = \frac{x + 4}{-2x^2 + 2x + 4}$$

Holes: None  
Horz. Asym.:  $y = 0$   
Domain: All reals except  $-1, 2$

$$42) \ f(x) = \frac{-2x^2 + 18}{x^2 - 5x + 6}$$

Holes:  $x = 3$   
Horz. Asym.:  $y = -2$   
Domain: All reals except  $2, 3$

$$43) \ f(x) = \frac{1}{-3x^2 + 12}$$

Holes: None  
Horz. Asym.:  $y = 0$   
Domain: All reals except  $-2, 2$

$$44) \ f(x) = \frac{1}{3x - 12}$$

Holes: None  
Horz. Asym.:  $y = 0$   
Domain: All reals except  $4$

$$45) \ f(x) = \frac{1}{-x}$$

Holes: None  
Horz. Asym.:  $y = 0$   
Domain: All reals except  $0$

$$46) \ f(x) = \frac{x - 4}{-x - 3}$$

Holes: None  
Horz. Asym.:  $y = -1$   
Domain: All reals except  $-3$

$$47) \ f(x) = \frac{-2x^3 + 4x^2}{x^3 - 6x^2 + 8x}$$

Holes:  $x = 0, x = 2$   
 Horz. Asym.:  $y = -2$   
 Domain: All reals except 0, 2, 4

$$48) \ f(x) = \frac{x^2 + 4x + 3}{-4x + 4}$$

Holes: None  
 Horz. Asym.: None  
 Domain: All reals except 1

$$49) \ f(x) = \frac{x}{x + 3}$$

Holes: None  
 Horz. Asym.:  $y = 1$   
 Domain: All reals except  $-3$

$$50) \ f(x) = \frac{x^3 + 5x^2 + 4x}{3x^2 + 6x - 9}$$

Holes: None  
 Horz. Asym.: None  
 Domain: All reals except  $-3, 1$

$$51) \ f(x) = \frac{x^2 + 5x + 6}{3x^2 - 3x - 6}$$

Holes: None  
 Horz. Asym.:  $y = \frac{1}{3}$   
 Domain: All reals except  $-1, 2$

$$52) \ f(x) = \frac{x^2 + 3x}{-4x^2 + 4x + 48}$$

Holes:  $x = -3$   
 Horz. Asym.:  $y = -\frac{1}{4}$   
 Domain: All reals except  $-3, 4$

$$53) \ f(x) = \frac{-3x^2 + 6x}{x^2 - 2x - 3}$$

Holes: None  
 Horz. Asym.:  $y = -3$   
 Domain: All reals except  $-1, 3$

$$54) \ f(x) = \frac{x}{-3x^2 - 9x}$$

Holes:  $x = 0$   
 Horz. Asym.:  $y = 0$   
 Domain: All reals except  $-3, 0$

$$55) \ f(x) = \frac{x^2 + x}{4x + 12}$$

Holes: None  
 Horz. Asym.: None  
 Domain: All reals except  $-3$

$$56) \ f(x) = \frac{-x^2 - x}{x^2 + x - 6}$$

Holes: None  
 Horz. Asym.:  $y = -1$   
 Domain: All reals except  $-3, 2$

$$57) \ f(x) = \frac{2}{x^2 - x - 2}$$

Holes: None  
 Horz. Asym.:  $y = 0$   
 Domain: All reals except  $-1, 2$

$$58) \ f(x) = \frac{x^3 + 3x^2 + 2x}{-3x^2 - 9x}$$

Holes:  $x = 0$   
 Horz. Asym.: None  
 Domain: All reals except  $-3, 0$

$$59) \ f(x) = \frac{x^2 - 9}{-x^2 + 5x - 6}$$

Holes:  $x = 3$   
 Horz. Asym.:  $y = -1$   
 Domain: All reals except 2, 3

$$60) \ f(x) = \frac{-x - 3}{x^2 + 4x + 3}$$

Holes:  $x = -3$   
 Horz. Asym.:  $y = 0$   
 Domain: All reals except  $-3, -1$

$$61) \ f(x) = \frac{-x^2 + 5x - 6}{x^2 + 2x - 3}$$

Holes: None  
 Horz. Asym.:  $y = -1$   
 Domain: All reals except  $-3, 1$

$$62) \ f(x) = \frac{1}{x^2 - 2x - 3}$$

Holes: None  
 Horz. Asym.:  $y = 0$   
 Domain: All reals except  $-1, 3$

$$63) \ f(x) = \frac{x^2 + 2x - 3}{4x^2 + 12x}$$

Holes:  $x = -3$   
 Horz. Asym.:  $y = \frac{1}{4}$   
 Domain: All reals except  $-3, 0$

$$64) \ f(x) = \frac{x + 1}{x - 3}$$

Holes: None  
 Horz. Asym.:  $y = 1$   
 Domain: All reals except 3

$$65) \ f(x) = \frac{x + 4}{3x - 12}$$

Holes: None  
 Horz. Asym.:  $y = \frac{1}{3}$   
 Domain: All reals except 4

$$66) \ f(x) = \frac{-3x - 9}{x^2 + 5x + 6}$$

Holes:  $x = -3$   
 Horz. Asym.:  $y = 0$   
 Domain: All reals except  $-3, -2$

$$67) \ f(x) = -\frac{2}{x^2 + 3x}$$

Holes: None  
 Horz. Asym.:  $y = 0$   
 Domain: All reals except  $-3, 0$

$$68) \ f(x) = \frac{2x^2 + 10x + 8}{x^2 - 1}$$

Holes:  $x = -1$   
 Horz. Asym.:  $y = 2$   
 Domain: All reals except  $-1, 1$

$$69) \ f(x) = \frac{-x^2 - x}{x^2 + x - 2}$$

Holes: None  
 Horz. Asym.:  $y = -1$   
 Domain: All reals except  $-2, 1$

$$70) \ f(x) = \frac{x^3 - 7x^2 + 12x}{-4x^2 + 12x + 16}$$

Holes:  $x = 4$   
 Horz. Asym.: None  
 Domain: All reals except  $-1, 4$

$$71) \ f(x) = \frac{x^3 + 2x^2 - 8x}{-4x^2 + 12x}$$

Holes:  $x = 0$   
Horz. Asym.: None  
Domain: All reals except 0, 3

$$72) \ f(x) = \frac{3x - 9}{x^3 - 5x^2 + 6x}$$

Holes:  $x = 3$   
Horz. Asym.:  $y = 0$   
Domain: All reals except 0, 2, 3

$$73) \ f(x) = \frac{x^2 + 4x}{-2x^2 - 4x + 6}$$

Holes: None  
Horz. Asym.:  $y = -\frac{1}{2}$   
Domain: All reals except -3, 1

$$75) \ f(x) = \frac{x^2 - 4x}{4x - 8}$$

Holes: None  
Horz. Asym.: None  
Domain: All reals except 2

$$74) \ f(x) = \frac{1}{x^2 + x - 6}$$

Holes: None  
Horz. Asym.:  $y = 0$   
Domain: All reals except -3, 2

$$77) \ f(x) = \frac{x^3 + 2x^2 - 3x}{4x^2 + 20x + 24}$$

Holes:  $x = -3$   
Horz. Asym.: None  
Domain: All reals except -3, -2

$$78) \ f(x) = \frac{1}{x + 2}$$

Holes: None  
Horz. Asym.:  $y = 0$   
Domain: All reals except -2

$$79) \ f(x) = \frac{x^3 - 6x^2 + 8x}{4x^2 - 12x}$$

Holes:  $x = 0$   
Horz. Asym.: None  
Domain: All reals except 0, 3

$$80) \ f(x) = \frac{x^2 + 3x + 2}{-3x - 12}$$

Holes: None  
Horz. Asym.: None  
Domain: All reals except -4