

1.) Find the distance between the points

$$\begin{array}{c} x_1 \quad y_1 \\ (2, 7) \end{array} \quad \begin{array}{c} x_2 \quad y_2 \\ (-7, -5) \end{array}$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$\sqrt{(-7 - 2)^2 + (7 - (-5))^2}$$

$$\sqrt{(-9)^2 + (12)^2}$$

$$\sqrt{81 + 144} = \sqrt{225} = \boxed{15}$$

2.) Find the midpoint between $(8, -6)$ and $(-2, 12)$

$$\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right) = \left(\frac{8 + (-2)}{2}, \frac{12 + (-6)}{2} \right)$$

$$\left(\frac{6}{2}, \frac{6}{2} \right)$$

$$(x - h)^2 + (y - k)^2 = r^2$$

$$\boxed{(3, 3)}$$

$$3.) \quad \underset{\downarrow}{(x+3)^2} + \underset{\downarrow}{(y-8)^2} = 81$$

Center: $(\underline{\underline{h}}, \underline{\underline{k}})$ radius = r

$$\sqrt{r^2} = \sqrt{81}$$

$$\boxed{(-3, 8) \quad r=9}$$

4.) Equation for circle with center $(2, -4)$
and radius = 8.

$$\boxed{(x - 2)^2 + (y + 4)^2 = 64}$$

$$x^2 + y^2 + 8x + 2y - 28 = 0 \quad |.) \text{ 2020 IT}$$

$$(x^2 + \boxed{8}x) + (y^2 + 2y) = 28$$

$\left(\frac{8}{2}\right)^2 + 16 \quad \left(\frac{2}{2}\right)^2 + 1 \quad + 16 + 1$

$$(4)^2 = 16 \quad (1)^2 = 1$$

$$(x^2 + 8x + 16) + (y^2 + 2y + 1) = 45$$

$\sqrt{x^2} \downarrow \quad \sqrt{16} \downarrow \quad \sqrt{y^2} \downarrow \quad \downarrow \sqrt{1}$

$$(x+4)^2 + (y+1)^2 = 45$$

Center: $(-4, -1)$ radius: $\sqrt{45} = \sqrt{9 \cdot 5} = 3\sqrt{5}$

2020 IT

$$\textcircled{3}x^2 + \textcircled{2}y^2 - 42x + 32y + 88 = 0$$

$$-88 = -88$$

$$(\textcircled{3}x^2 - \frac{42}{3}x) + (\textcircled{2}y^2 + \frac{32}{2}y) = -88$$

$$\textcircled{3}(x^2 - 14x) + \textcircled{2}(y^2 + 16y) = -88 + 147 + 128$$

$\left(\frac{14}{2}\right)^2 + 49 \quad \left(\frac{16}{2}\right)^2 + 64 \quad + 3(49) + 2(64)$

$$3(x^2 - 14x + 49) + 2(y^2 + 16y + 64) = 187$$

$$3(x-7)^2 + 2(y+8)^2 = 187$$

Center: $(7, -8)$ radius: $\sqrt{187}$

$$x^2 - 8x + y^2 + 20y + 107 = 0$$

$-107 \quad -107$

$$\left\{ \begin{array}{l} (x^2 - 8x) + (y^2 + 20y) = -107 \\ \left(\frac{-8}{2} \right)^2 + 16 \quad \left(\frac{20}{2} \right)^2 + 100 \quad + 16 \quad + 100 \\ 4^2 = 16 \quad 10^2 = 100 \end{array} \right.$$

$-107 + 16 + 100 = 9$

$$(x^2 - 8x + 16) + (y^2 + 20 + 100) = 9$$

$$\sqrt{x^2} - 8x + 16 + \sqrt{16} + (y + 10)^2 = 9$$

$$(x - 4)^2 + (y + 10)^2 = 9$$

Center: $(4, -10)$ radius: 3

Find the slope

$$\text{slope } m = \frac{\text{rise}}{\text{run}} = \frac{\Delta y}{\Delta x} = \frac{y_2 - y_1}{x_2 - x_1}$$

$$(x_2, y_2) \quad (x_1, y_1)$$

$$(1, 3) \quad (5, 9)$$

$$\frac{3 - 9}{1 - 5} = \frac{-6}{-4} = \boxed{\frac{3}{2}}$$

$$(2, -8) \quad (6, 4)$$

$$\frac{y_2 - y_1}{x_2 - x_1} = \frac{-8 - 4}{2 - 6} = \frac{-12}{-4} = \boxed{3}$$

Slope- Intercept form

$$y = mx + b$$

$$\text{slope} = \frac{2}{3}$$

$$y\text{-int} = 4$$

$$y = \frac{2}{3}x + 4$$

Point-Slope form: $(x_2 - x_1)m = \frac{y_2 - y_1}{x_2 - x_1} (x - x_1)$

Equation for a

line

$$m = -\frac{3}{2}$$

through $(4, 2)$

$$(x_1, y_1)$$

$$\left. \begin{array}{l} y_2 - y_1 = m(x_2 - x_1) \\ y - y_1 = m(x - x_1) \\ y - 2 = -\frac{3}{2}(x + 4) \end{array} \right\}$$

$$y = mx + b$$

$$2 = \left(-\frac{3}{2}\right)(-4) + b$$

$$2 = \frac{12}{2} + b$$

$$2 = 6 + b$$

$$b = -4$$

$$y = mx + b$$

$$y = -\frac{3}{2}x - 4$$

Find equation slope = -3 through (-2, 4)

$$y = mx + b$$

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$$4 = (-3)(-2) + b$$

$$4 = b + b$$

$$-6 - b$$

$$-2 = b$$

point-slope form

$$y - y_1 = m(x - x_1)$$

$$y - 4 = -3(x + 2)$$

$$\boxed{y = mx + b}$$
$$\boxed{y = -3x - 2}$$

Equation ~~(4, -2)~~ and ~~(-2, -5)~~

$$\text{slope} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-2 - (-5)}{4 + (-2)} = \frac{3}{6} = \frac{1}{2} = m$$

$$y = mx + b$$

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$$-2 = \left(\frac{1}{2}\right)(4) + b$$

$$-2 = 2 + b$$

$$-2 - 2$$

$$-4 = b$$

(4, -2)

$$y = mx + b$$

$$\boxed{y = \frac{1}{2}x - 4}$$

