

$$f(x) = \frac{x+1}{x^2+3x}$$

$$f(x) = \frac{x+1}{x(x+3)}$$

$$x \neq 0$$

$$x+3=0$$

$$\begin{matrix} -3 & -3 \\ \hline \end{matrix}$$

$$x \neq -3$$

vertical asymptotes: $x=0, x=-3$

holes no holes

horizontal asymptotes
limits to infinity

Domain

$$x \neq 0, x \neq -3$$

$$\frac{\cancel{x+1}}{x(\cancel{x+1})} \quad x = -1 \text{ holes}$$

$$\frac{*}{x^2} = \frac{1}{x}$$

$$\lim_{x \rightarrow \infty} \frac{1}{x} = \frac{1}{\infty} = 0 \quad \text{horizontal asymptote}$$

$$\frac{3x^2}{4x^2} = \text{highest degree terms same, horizontal asymptote is equal to the ratio of coefficients. } \left(\frac{3}{4}\right)$$

$$\frac{3x^2}{4x} \Rightarrow \text{Top Heavy} \rightarrow \text{infinity}$$

$$\frac{3x}{4x^2} \Rightarrow \text{Bottom Heavy} \rightarrow \emptyset$$

$$\frac{x^2 - 16}{x^2 + 2x - 8}$$

$$x^2 + 2x - 8 \neq 0$$

$$(x+4)(x-2) \neq 0$$

$$\begin{array}{cc} \downarrow & \downarrow \\ x+4 \neq 0 & x-2 \neq 0 \\ -4 & +2 \quad +2 \\ x \neq -4 & x \neq 2 \end{array}$$

Domain

Vertical Asymptote
or
Hole

$$\frac{7}{0} \\ \uparrow \\ \text{undefined}$$

Horizontal Asymptote

Domain

$x \neq -4$ $x \neq 2$ — vertical asymptote
hole

$$x^2 - 16 = \frac{(x+4)(x-4)}{(x+4)(x-2)}$$

$$\frac{1}{1} = 1$$