

Assignment

Date _____ Period _____

State the possible rational zeros for each function. Then find all rational zeros.

1) $f(x) = 2x^3 - 9x^2 - 43x - 20$

2) $f(x) = 2x^3 - 15x^2 - 16x - 4$

3) $f(x) = x^3 + x^2 + 4x - 20$

4) $f(x) = 6x^3 + 28x^2 + 25x + 6$

5) $f(x) = x^3 + 2x^2 - x - 2$

6) $f(x) = 3x^3 - 10x^2 - 18x + 7$

7) $f(x) = x^3 - 3x^2 - x + 3$

8) $f(x) = 3x^3 + 34x^2 - 57x + 22$

9) $f(x) = 4x^3 - x^2 - 4x + 1$

10) $f(x) = 3x^3 + 5x^2 - 11x + 3$

$$11) \ f(x) = 3x^3 + x^2 - 5x + 10$$

$$12) \ f(x) = 4x^3 + x^2 - 4x - 1$$

$$13) \ f(x) = 3x^3 - x^2 - 3x + 1$$

$$14) \ f(x) = 3x^3 - 5x^2 + x + 1$$

$$15) \ f(x) = 2x^3 + 17x^2 + 36x + 5$$

$$16) \ f(x) = 6x^3 + 11x^2 - 2x - 3$$

$$17) \ f(x) = 2x^3 - x^2 - 5x - 2$$

$$18) \ f(x) = 6x^3 + x^2 - 11x - 5$$

$$19) \ f(x) = x^3 - 6x^2 - 11x + 10$$

$$20) \ f(x) = x^3 - 5x^2 - x + 5$$

$$21) \ f(x) = x^3 - 4x^2 - 11x + 2$$

$$22) \ f(x) = 2x^3 + x^2 - 5x + 2$$

$$23) \ f(x) = 5x^3 + x^2 - 5x - 1$$

$$24) \ f(x) = 3x^3 + 17x^2 - 24x + 6$$

$$25) \ f(x) = x^3 + 3x^2 - 20$$

$$26) \ f(x) = 4x^3 - 9x^2 + 6x - 1$$

$$27) \ f(x) = 5x^3 + 59x^2 - 17x + 1$$

$$28) \ f(x) = 3x^3 - 8x^2 + 5x - 2$$

$$29) \ f(x) = 5x^3 + 9x^2 + 3x - 1$$

$$30) \ f(x) = x^3 - 12x^2 + 30x - 9$$

$$31) \ f(x) = x^3 + 12x^2 + 15x - 10$$

$$32) \ f(x) = x^3 + 2x^2 + 3x + 18$$

$$33) \ f(x) = 6x^3 + 23x^2 + 2x - 4$$

$$34) \ f(x) = x^3 + 5x^2 - x - 5$$

$$35) \ f(x) = x^3 + 5x^2 - 6x - 24$$

$$36) \ f(x) = 5x^3 - 11x^2 + 7x - 1$$

$$37) \ f(x) = 2x^3 - 3x^2 + 1$$

$$38) \ f(x) = 3x^3 + 35x^2 - 4$$

$$39) \ f(x) = x^3 - 3x + 2$$

$$40) \ f(x) = 2x^3 - 7x^2 + 7x - 2$$

$$41) \ f(x) = 4x^3 - 27x + 5$$

$$42) \ f(x) = 2x^3 + 3x^2 - 1$$

$$43) \ f(x) = x^3 - 4x^2 - 5x + 14$$

$$44) \ f(x) = 5x^3 + 19x^2 - 29x + 5$$

$$45) \ f(x) = 2x^3 - 3x^2 - 26x + 3$$

$$46) \ f(x) = 2x^3 - 12x^2 + 23x - 14$$

$$47) \ f(x) = 2x^3 + 27x^2 + 57x + 5$$

$$48) \ f(x) = 2x^3 - 14x^2 + 29x - 18$$

$$49) \ f(x) = 2x^3 + 4x^2 - 9x - 14$$

$$50) \ f(x) = 6x^3 + 32x^2 + 31x + 7$$

$$51) \ f(x) = 3x^3 + x^2 - 3x - 1$$

$$52) \ f(x) = 3x^3 - 11x^2 - 22x - 6$$

$$53) \ f(x) = 3x^3 - 23x^2 + 49x - 45$$

$$54) \ f(x) = 3x^3 + 5x^2 + x - 1$$

$$55) \ f(x) = 3x^3 + 7x^2 + 5x + 1$$

$$56) \ f(x) = x^3 + 2x^2 - 32x - 15$$

$$57) \ f(x) = x^3 + 14x^2 + 29x + 10$$

$$58) \ f(x) = 2x^3 - x^2 - 2x + 1$$

$$59) \ f(x) = 2x^3 + x^2 - 2x - 1$$

$$60) \ f(x) = 2x^3 + 5x^2 + 4x + 1$$

Assignment

Date _____ Period _____

State the possible rational zeros for each function. Then find all rational zeros.

1) $f(x) = 2x^3 - 9x^2 - 43x - 20$

Possible rational zeros:

$$\pm 1, \pm 2, \pm 4, \pm 5, \pm 10, \pm 20, \pm \frac{1}{2}, \pm \frac{5}{2}$$

$$\text{Rational zeros: } \left\{-\frac{5}{2}\right\}$$

2) $f(x) = 2x^3 - 15x^2 - 16x - 4$

Possible rational zeros: $\pm 1, \pm 2, \pm 4, \pm \frac{1}{2}$

$$\text{Rational zeros: } \left\{-\frac{1}{2}\right\}$$

3) $f(x) = x^3 + x^2 + 4x - 20$

Possible rational zeros:

$$\pm 1, \pm 2, \pm 4, \pm 5, \pm 10, \pm 20$$

$$\text{Rational zeros: } \{2\}$$

4) $f(x) = 6x^3 + 28x^2 + 25x + 6$

Possible rational zeros:

$$\pm 1, \pm 2, \pm 3, \pm 6, \pm \frac{1}{2}, \pm \frac{3}{2}, \pm \frac{1}{3}, \pm \frac{2}{3}, \pm \frac{1}{6}$$

$$\text{Rational zeros: } \left\{-\frac{2}{3}\right\}$$

5) $f(x) = x^3 + 2x^2 - x - 2$

Possible rational zeros: $\pm 1, \pm 2$

$$\text{Rational zeros: } \{-2, -1, 1\}$$

6) $f(x) = 3x^3 - 10x^2 - 18x + 7$

Possible rational zeros: $\pm 1, \pm 7, \pm \frac{1}{3}, \pm \frac{7}{3}$

$$\text{Rational zeros: } \left\{\frac{1}{3}\right\}$$

7) $f(x) = x^3 - 3x^2 - x + 3$

Possible rational zeros: $\pm 1, \pm 3$

$$\text{Rational zeros: } \{3, 1, -1\}$$

8) $f(x) = 3x^3 + 34x^2 - 57x + 22$

Possible rational zeros:

$$\pm 1, \pm 2, \pm 11, \pm 22, \pm \frac{1}{3}, \pm \frac{2}{3}, \pm \frac{11}{3}, \pm \frac{22}{3}$$

$$\text{Rational zeros: } \left\{\frac{2}{3}\right\}$$

9) $f(x) = 4x^3 - x^2 - 4x + 1$

Possible rational zeros: $\pm 1, \pm \frac{1}{2}, \pm \frac{1}{4}$

$$\text{Rational zeros: } \left\{\frac{1}{4}, 1, -1\right\}$$

10) $f(x) = 3x^3 + 5x^2 - 11x + 3$

Possible rational zeros: $\pm 1, \pm 3, \pm \frac{1}{3}$

$$\text{Rational zeros: } \left\{\frac{1}{3}, -3, 1\right\}$$

$$11) \ f(x) = 3x^3 + x^2 - 5x + 10$$

Possible rational zeros:

$$\pm 1, \pm 2, \pm 5, \pm 10, \pm \frac{1}{3}, \pm \frac{2}{3}, \pm \frac{5}{3}, \pm \frac{10}{3}$$

Rational zeros: $\{-2\}$

$$13) \ f(x) = 3x^3 - x^2 - 3x + 1$$

Possible rational zeros: $\pm 1, \pm \frac{1}{3}$

Rational zeros: $\left\{-1, 1, \frac{1}{3}\right\}$

$$15) \ f(x) = 2x^3 + 17x^2 + 36x + 5$$

Possible rational zeros: $\pm 1, \pm 5, \pm \frac{1}{2}, \pm \frac{5}{2}$

Rational zeros: $\{-5\}$

$$17) \ f(x) = 2x^3 - x^2 - 5x - 2$$

Possible rational zeros: $\pm 1, \pm 2, \pm \frac{1}{2}$

Rational zeros: $\left\{-\frac{1}{2}, -1, 2\right\}$

$$19) \ f(x) = x^3 - 6x^2 - 11x + 10$$

Possible rational zeros: $\pm 1, \pm 2, \pm 5, \pm 10$

Rational zeros: $\{-2\}$

$$12) \ f(x) = 4x^3 + x^2 - 4x - 1$$

Possible rational zeros: $\pm 1, \pm \frac{1}{2}, \pm \frac{1}{4}$

Rational zeros: $\left\{-\frac{1}{4}, 1, -1\right\}$

$$14) \ f(x) = 3x^3 - 5x^2 + x + 1$$

Possible rational zeros: $\pm 1, \pm \frac{1}{3}$

Rational zeros: $\left\{-\frac{1}{3}, 1 \text{ mult. 2}\right\}$

$$16) \ f(x) = 6x^3 + 11x^2 - 2x - 3$$

Possible rational zeros:

$$\pm 1, \pm 3, \pm \frac{1}{2}, \pm \frac{3}{2}, \pm \frac{1}{3}, \pm \frac{1}{6}$$

Rational zeros: $\left\{-\frac{1}{2}\right\}$

$$18) \ f(x) = 6x^3 + x^2 - 11x - 5$$

Possible rational zeros:

$$\pm 1, \pm 5, \pm \frac{1}{2}, \pm \frac{5}{2}, \pm \frac{1}{3}, \pm \frac{5}{3}, \pm \frac{1}{6}, \pm \frac{5}{6}$$

Rational zeros: $\left\{-\frac{1}{2}\right\}$

$$20) \ f(x) = x^3 - 5x^2 - x + 5$$

Possible rational zeros: $\pm 1, \pm 5$

Rational zeros: $\{1, 5, -1\}$

$$21) \ f(x) = x^3 - 4x^2 - 11x + 2$$

Possible rational zeros: $\pm 1, \pm 2$
Rational zeros: $\{-2\}$

$$22) \ f(x) = 2x^3 + x^2 - 5x + 2$$

Possible rational zeros: $\pm 1, \pm 2, \pm \frac{1}{2}$
Rational zeros: $\left\{1, \frac{1}{2}, -2\right\}$

$$23) \ f(x) = 5x^3 + x^2 - 5x - 1$$

Possible rational zeros: $\pm 1, \pm \frac{1}{5}$
Rational zeros: $\left\{-\frac{1}{5}, 1, -1\right\}$

$$24) \ f(x) = 3x^3 + 17x^2 - 24x + 6$$

Possible rational zeros:
 $\pm 1, \pm 2, \pm 3, \pm 6, \pm \frac{1}{3}, \pm \frac{2}{3}$
Rational zeros: $\left\{\frac{1}{3}\right\}$

$$25) \ f(x) = x^3 + 3x^2 - 20$$

Possible rational zeros:
 $\pm 1, \pm 2, \pm 4, \pm 5, \pm 10, \pm 20$
Rational zeros: $\{2\}$

$$26) \ f(x) = 4x^3 - 9x^2 + 6x - 1$$

Possible rational zeros: $\pm 1, \pm \frac{1}{2}, \pm \frac{1}{4}$
Rational zeros: $\left\{1 \text{ mult. } 2, \frac{1}{4}\right\}$

$$27) \ f(x) = 5x^3 + 59x^2 - 17x + 1$$

Possible rational zeros: $\pm 1, \pm \frac{1}{5}$
Rational zeros: $\left\{\frac{1}{5}\right\}$

$$28) \ f(x) = 3x^3 - 8x^2 + 5x - 2$$

Possible rational zeros: $\pm 1, \pm 2, \pm \frac{1}{3}, \pm \frac{2}{3}$
Rational zeros: $\{2\}$

$$29) \ f(x) = 5x^3 + 9x^2 + 3x - 1$$

Possible rational zeros: $\pm 1, \pm \frac{1}{5}$
Rational zeros: $\left\{\frac{1}{5}, -1 \text{ mult. } 2\right\}$

$$30) \ f(x) = x^3 - 12x^2 + 30x - 9$$

Possible rational zeros: $\pm 1, \pm 3, \pm 9$
Rational zeros: $\{3\}$

$$31) \ f(x) = x^3 + 12x^2 + 15x - 10$$

Possible rational zeros: $\pm 1, \pm 2, \pm 5, \pm 10$

Rational zeros: $\{-2\}$

$$32) \ f(x) = x^3 + 2x^2 + 3x + 18$$

Possible rational zeros:

$\pm 1, \pm 2, \pm 3, \pm 6, \pm 9, \pm 18$

Rational zeros: $\{-3\}$

$$33) \ f(x) = 6x^3 + 23x^2 + 2x - 4$$

Possible rational zeros:

$\pm 1, \pm 2, \pm 4, \pm \frac{1}{2}, \pm \frac{1}{3}, \pm \frac{2}{3}, \pm \frac{4}{3}, \pm \frac{1}{6}$

Rational zeros: $\left\{-\frac{1}{2}\right\}$

$$34) \ f(x) = x^3 + 5x^2 - x - 5$$

Possible rational zeros: $\pm 1, \pm 5$

Rational zeros: $\{-5, -1, 1\}$

$$35) \ f(x) = x^3 + 5x^2 - 6x - 24$$

Possible rational zeros:

$\pm 1, \pm 2, \pm 3, \pm 4, \pm 6, \pm 8, \pm 12, \pm 24$

Rational zeros: $\{-2\}$

$$36) \ f(x) = 5x^3 - 11x^2 + 7x - 1$$

Possible rational zeros: $\pm 1, \pm \frac{1}{5}$

Rational zeros: $\left\{\frac{1}{5}, 1 \text{ mult. 2}\right\}$

$$37) \ f(x) = 2x^3 - 3x^2 + 1$$

Possible rational zeros: $\pm 1, \pm \frac{1}{2}$

Rational zeros: $\left\{-\frac{1}{2}, 1 \text{ mult. 2}\right\}$

$$38) \ f(x) = 3x^3 + 35x^2 - 4$$

Possible rational zeros:

$\pm 1, \pm 2, \pm 4, \pm \frac{1}{3}, \pm \frac{2}{3}, \pm \frac{4}{3}$

Rational zeros: $\left\{\frac{1}{3}\right\}$

$$39) \ f(x) = x^3 - 3x + 2$$

Possible rational zeros: $\pm 1, \pm 2$

Rational zeros: $\{-2, 1 \text{ mult. 2}\}$

$$40) \ f(x) = 2x^3 - 7x^2 + 7x - 2$$

Possible rational zeros: $\pm 1, \pm 2, \pm \frac{1}{2}$

Rational zeros: $\left\{1, 2, \frac{1}{2}\right\}$

41) $f(x) = 4x^3 - 27x + 5$

Possible rational zeros:

$$\pm 1, \pm 5, \pm \frac{1}{2}, \pm \frac{5}{2}, \pm \frac{1}{4}, \pm \frac{5}{4}$$

Rational zeros: $\left\{\frac{5}{2}\right\}$

43) $f(x) = x^3 - 4x^2 - 5x + 14$

Possible rational zeros: $\pm 1, \pm 2, \pm 7, \pm 14$

Rational zeros: $\{-2\}$

45) $f(x) = 2x^3 - 3x^2 - 26x + 3$

Possible rational zeros: $\pm 1, \pm 3, \pm \frac{1}{2}, \pm \frac{3}{2}$

Rational zeros: $\{-3\}$

47) $f(x) = 2x^3 + 27x^2 + 57x + 5$

Possible rational zeros: $\pm 1, \pm 5, \pm \frac{1}{2}, \pm \frac{5}{2}$

Rational zeros: $\left\{-\frac{5}{2}\right\}$

49) $f(x) = 2x^3 + 4x^2 - 9x - 14$

Possible rational zeros:

$$\pm 1, \pm 2, \pm 7, \pm 14, \pm \frac{1}{2}, \pm \frac{7}{2}$$

Rational zeros: $\{2\}$

42) $f(x) = 2x^3 + 3x^2 - 1$

Possible rational zeros: $\pm 1, \pm \frac{1}{2}$

Rational zeros: $\left\{\frac{1}{2}, -1 \text{ mult. 2}\right\}$

44) $f(x) = 5x^3 + 19x^2 - 29x + 5$

Possible rational zeros: $\pm 1, \pm 5, \pm \frac{1}{5}$

Rational zeros: $\left\{\frac{1}{5}, 1, -5\right\}$

46) $f(x) = 2x^3 - 12x^2 + 23x - 14$

Possible rational zeros:

$$\pm 1, \pm 2, \pm 7, \pm 14, \pm \frac{1}{2}, \pm \frac{7}{2}$$

Rational zeros: $\{2\}$

48) $f(x) = 2x^3 - 14x^2 + 29x - 18$

Possible rational zeros:

$$\pm 1, \pm 2, \pm 3, \pm 6, \pm 9, \pm 18, \pm \frac{1}{2}, \pm \frac{3}{2}, \pm \frac{9}{2}$$

Rational zeros: $\{2\}$

50) $f(x) = 6x^3 + 32x^2 + 31x + 7$

Possible rational zeros:

$$\pm 1, \pm 7, \pm \frac{1}{2}, \pm \frac{7}{2}, \pm \frac{1}{3}, \pm \frac{7}{3}, \pm \frac{1}{6}, \pm \frac{7}{6}$$

Rational zeros: $\left\{-\frac{1}{3}\right\}$

51) $f(x) = 3x^3 + x^2 - 3x - 1$

Possible rational zeros: $\pm 1, \pm \frac{1}{3}$

Rational zeros: $\left\{1, -1, -\frac{1}{3}\right\}$

53) $f(x) = 3x^3 - 23x^2 + 49x - 45$

Possible rational zeros:

$\pm 1, \pm 3, \pm 5, \pm 9, \pm 15, \pm 45, \pm \frac{1}{3}, \pm \frac{5}{3}$

Rational zeros: $\{5\}$

55) $f(x) = 3x^3 + 7x^2 + 5x + 1$

Possible rational zeros: $\pm 1, \pm \frac{1}{3}$

Rational zeros: $\left\{-\frac{1}{3}, -1 \text{ mult. 2}\right\}$

57) $f(x) = x^3 + 14x^2 + 29x + 10$

Possible rational zeros: $\pm 1, \pm 2, \pm 5, \pm 10$
Rational zeros: $\{-2\}$

59) $f(x) = 2x^3 + x^2 - 2x - 1$

Possible rational zeros: $\pm 1, \pm \frac{1}{2}$

Rational zeros: $\left\{1, -\frac{1}{2}, -1\right\}$

52) $f(x) = 3x^3 - 11x^2 - 22x - 6$

Possible rational zeros:

$\pm 1, \pm 2, \pm 3, \pm 6, \pm \frac{1}{3}, \pm \frac{2}{3}$

Rational zeros: $\left\{-\frac{1}{3}\right\}$

54) $f(x) = 3x^3 + 5x^2 + x - 1$

Possible rational zeros: $\pm 1, \pm \frac{1}{3}$

Rational zeros: $\left\{-1 \text{ mult. 2}, \frac{1}{3}\right\}$

56) $f(x) = x^3 + 2x^2 - 32x - 15$

Possible rational zeros: $\pm 1, \pm 3, \pm 5, \pm 15$
Rational zeros: $\{5\}$

58) $f(x) = 2x^3 - x^2 - 2x + 1$

Possible rational zeros: $\pm 1, \pm \frac{1}{2}$

Rational zeros: $\left\{-1, \frac{1}{2}, 1\right\}$

60) $f(x) = 2x^3 + 5x^2 + 4x + 1$

Possible rational zeros: $\pm 1, \pm \frac{1}{2}$

Rational zeros: $\left\{-1 \text{ mult. 2}, -\frac{1}{2}\right\}$