

M - A2 Algebra 2 Week 9

11/6

| x | y |
|---|---|
| 0 | 2 |
| 2 | 4 |
| 3 | 6 |
| 4 |   |

function

Each input  
has one, and  
only one, output.

| x | y   |
|---|-----|
| 0 | -3  |
| 1 | -6  |
| 4 | -18 |
|   | -24 |

not function

3.)  $(1, 4), (2, 5), (3, 8), (2, -6)$   
not function

4.)  $(-1, 3), (0, 8), (2, 18), (-3, -7)$

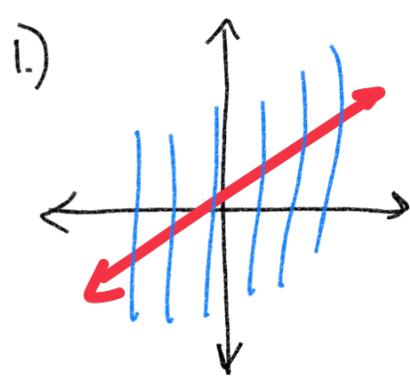
function

Domain:  $\{-1, 0, 2, -3\}$

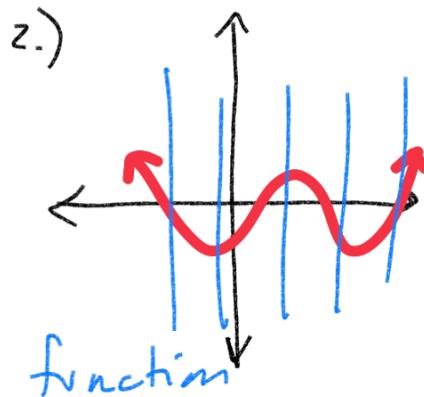
Range:  $\{3, 8, 18, -7\}$

Domain:  $\{0, 2, 3, 4\}$

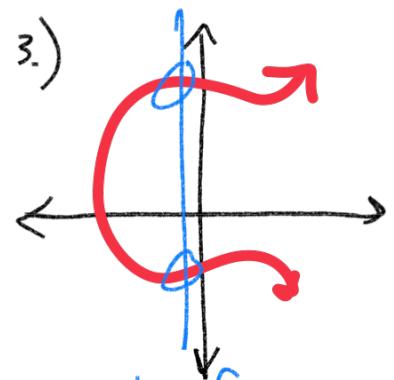
Range:  $\{2, 4, 6\}$



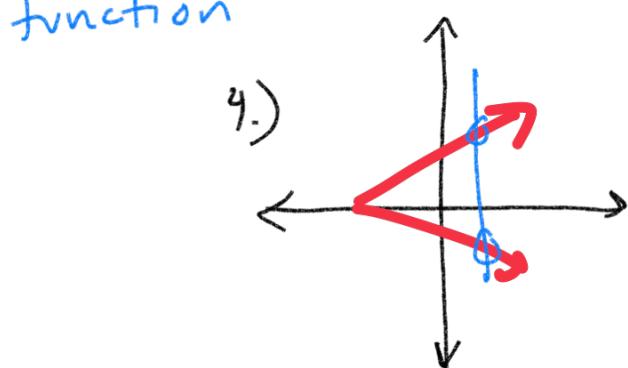
function



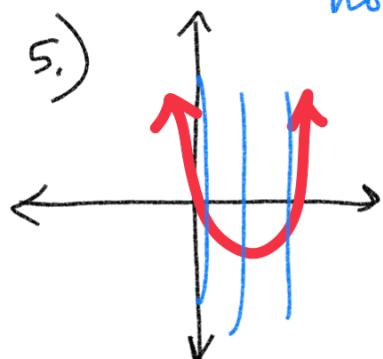
function



not function



not function



function

$$f(x) = 3x^2 + 6x + 12$$

$$f(-1) = 3(-1)^2 + 6(-1) + 12$$

$$3(1) + 6(-1) + 12$$

$$3 - 6 + 12$$

$$-3 + 12 = \boxed{9}$$

input  $\rightarrow -1$   
output  $\rightarrow 9$

$(-1, 9)$

$$f(4) = 3(4)^2 + 6(4) + 12$$

$$3(16) + 6(4) + 12$$

$$48 + 24 + 12$$

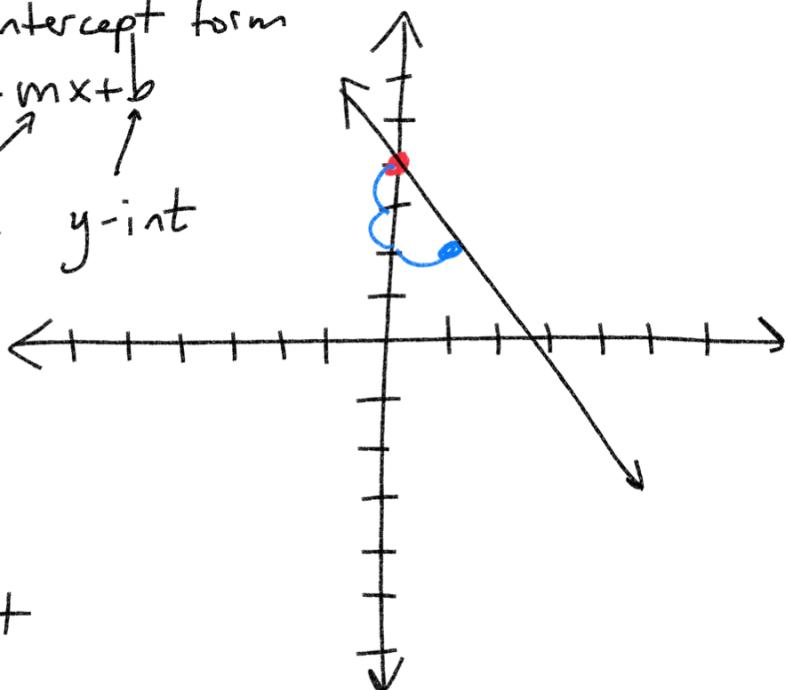
$$72 + 12 = 84$$

input  $\rightarrow 4$   
output  $\rightarrow 84$   
 $(4, 84)$

$$f(x) = -2x + 4$$

slope-intercept form  
 $y = mx + b$   
 slope      y-int

1) Plot y-int

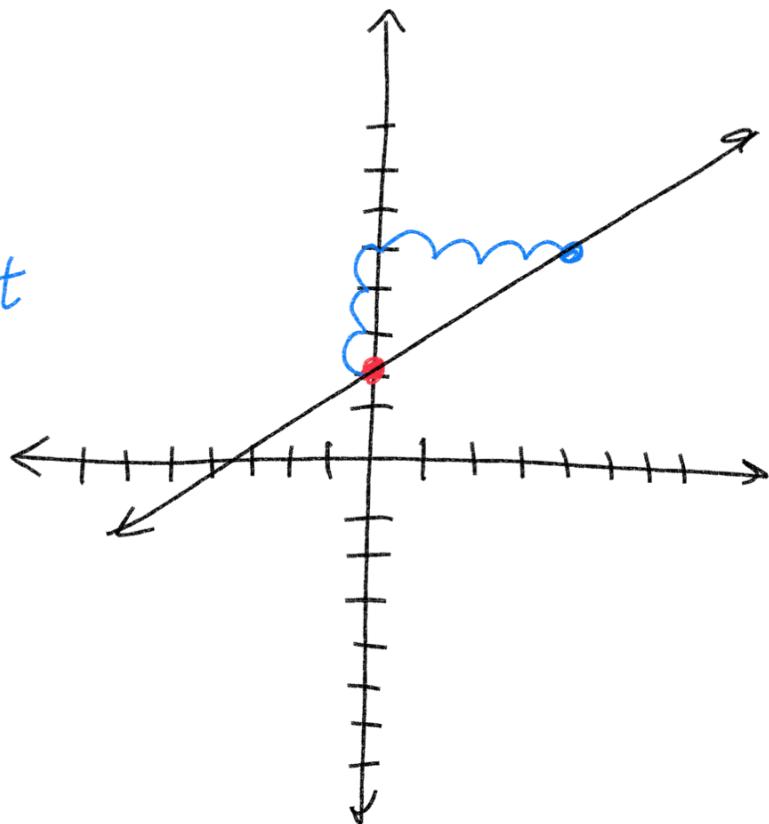


2) Use slope

$$\text{slope} = \frac{-2}{1} = \frac{2 \text{ down}}{1 \text{ right}}$$

$$f(x) = \frac{3}{4}x + 2$$

slope =  $\frac{3}{4}$  =  $\frac{\text{up } 3}{\text{right}}$



Standard Form

$$Ax + By = C$$

$$4x + 3y = 12$$

$$\cancel{4x} + 3y = 12$$

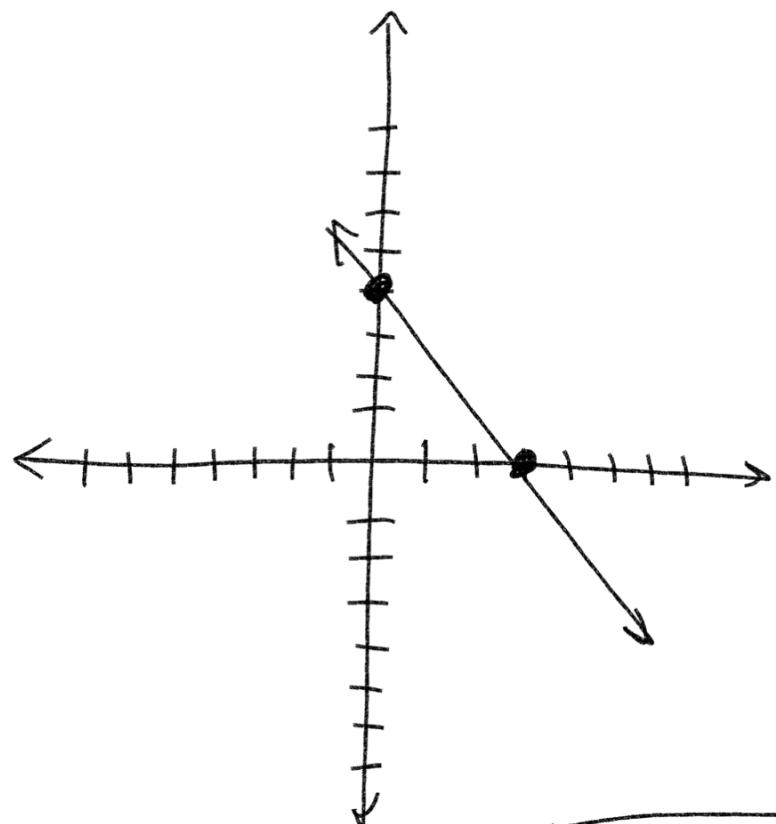
$x=0$        $\cancel{3y} = \frac{12}{3}$

$y = 4$        $(0, 4)$

$$4x + \cancel{3y} = 12$$

$y=0$        $4x = \frac{12}{4}$

$x = 3$        $(3, 0)$



$$\begin{aligned} 4x + 3y &= 12 \\ -4x & \\ \hline 3y &= -4x + 12 \end{aligned}$$

$$\boxed{y = -\frac{4}{3}x + 4}$$

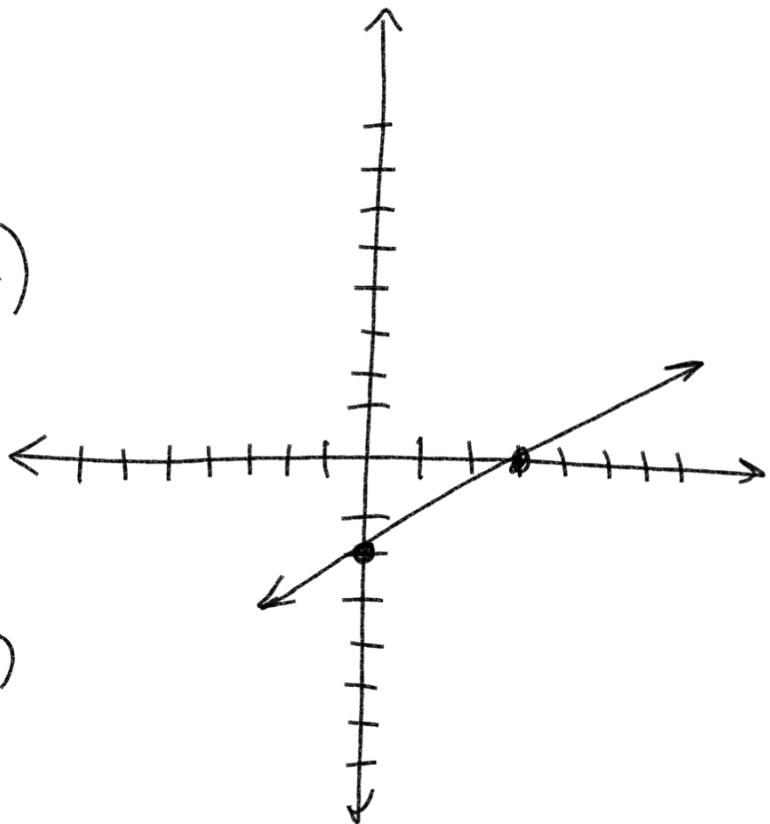
$$6x - 9y = 18$$

$$\cancel{6x} - \frac{9y}{-9} = \frac{18}{-9} \quad (0, -2)$$

$$y = -2$$

$$\frac{6x}{6} - \cancel{9y} = \frac{18}{6} \quad (3, 0)$$

$$x = 3$$



$$\text{slope} = \frac{\text{rise}}{\text{run}} = \frac{\Delta y}{\Delta x} = \frac{y_2 - y_1}{x_2 - x_1}$$

$$(4, 3) \quad (6, 9) \\ x_1, y_1 \quad x_2, y_2$$

$$\text{slope} = \frac{9 - 3}{6 - 4} = \frac{6}{2} = \boxed{3}$$

$$(4, 3) \quad (6, 9) \\ x_2, y_2 \quad x_1, y_1$$

$$\text{slope} = \frac{3 - 9}{4 - 6} = \frac{-6}{-2} = \boxed{3}$$

Find slope. (1, 3) (5, 11)

$$\text{slope} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{11 - 3}{5 - 1} = \frac{8}{4} = \boxed{2}$$

$$m = \text{slope} = \frac{y_2 - y_1}{x_2 - x_1} (x_2 - x_1) m = \left( \frac{y_2 - y_1}{x_2 - x_1} \right) (x_2 - x_1)$$

$$y_2 - y_1 = m(x_2 - x_1)$$

$$y = mx + b$$

$$y - y_1 = m(x - x_1)$$

slope-intercept form      point-slope form

Find the equation for a line with  $m = 4$   
that contains  $(3, 2)$

option #1 point-slope

$$y - y_1 = m(x - x_1)$$

$$\downarrow \quad \downarrow \quad \downarrow \quad \downarrow$$

$$y - 2 = 4(x - 3)$$

$$y - 2 = 4x - 12$$

$$+2 \qquad \qquad +2$$

$$\boxed{y = 4x - 10}$$

option #2 slope-int

$$y = mx + b$$

$$\downarrow \quad \downarrow$$

$$2 = (4)(3) + b$$

$$2 = 12 + b$$

$$-12 \quad -12$$

$$\boxed{-10 = b}$$

$$y = mx + b$$

$$\boxed{y = 4x - 10}$$

Find the equation for a line with  $m = -\frac{1}{2}$   
that contains  $(8, -2)$

Option #1

$$y - y_1 = m(x - x_1)$$

$$\downarrow \quad \downarrow \quad \downarrow$$

$$y - (-2) = -\frac{1}{2}(x - 8)$$

$$y + 2 = -\frac{1}{2}x + 4$$

$$\quad -2 \qquad \quad -2$$

$$\boxed{y = -\frac{1}{2}x + 2}$$

Option #2

$$y = mx + b$$

$$\downarrow \quad \downarrow \quad \downarrow$$

$$-2 = -\frac{1}{2}(8) + b$$

$$\begin{array}{rcl} -2 & = & -4 + b \\ +4 & & +4 \\ \hline 2 & = & b \end{array}$$

$$\boxed{y = -\frac{1}{2}x + 2}$$

Find the equation for a line  
through the points  $(2, 8)$  and  $\boxed{(3, -2)}$

1.) Find slope

2.) Find the equation

$$\text{slope} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-2 - 8}{3 - 2} = \frac{-10}{1} = -10 \quad m = -10$$

$$y - y_1 = m(x - x_1)$$

$$y - 8 = -10(\overbrace{x - 2})$$

$$y - 8 = -10x + 20$$

$$\boxed{y = -10x + 28}$$

$$y = mx + b$$

$$-2 = -10(3) + b$$

$$-2 = -30 + b$$

$$+30 \qquad +30 \qquad y = mx + b$$

$$28 = b$$

$$\boxed{y = -10x + 28}$$

